



#### Demagnetization Dynamics and Spin-dependent Lifetimes in Ferromagnets

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#### Thanks

#### Theory

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# Outline

- 1. Introduction & What is ultrafast demagnetization in ferromagnets?
- 2. Elliott-Yafet mechanism for electron-phonon scattering and dynamical Stoner model
- 3. Spin-dependent lifetimes in ferromagnets
- 4. Spin-dependent transport (in normal metals)

#### How Small & Fast Can Magnetism/Spintronics Get?



# Magnetization Dynamics: Scenarios in Fe, Co, Ni



Optically induced magnetization dynamics



Beaurepaire, Merle, Daunois, Bigot, Phys. Rev. Lett. 76, 4250 (1996)

### Magneto-Optical Kerr Effect: MOKE

- Magneto-optical effects: dielectric function depends on magnetization ε = ε(M)
- Influences reflected (Kerr effect) and transmitted light (Faraday effect) and
- MOKE: Light polarization angle rotated by  $\Theta_F(M)$
- Faraday geometry: Intensity changes = magnetic contrast



#### **Experimental TR-MOKE setup**



# **Ultrafast Demagnetization in Experiment**

- Pump-Probe-Measurement of the Magneto-optical Kerr Effect (MOKE)
- Magnetization changes on ultrafast timescales ("quenching")
- No coherent artifacts
- MOKE measures magnetization on ultrashort timescales



Beaurepaire, Merle, Daunois, Bigot, Phys. Rev. Lett. **76**, 4250 (1996) these data: M. Krauß et al., Phys. Rev. B **80**, 180407(R) (2009)

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# **Ultrafast Demagnetization in Experiment**

X-ray magnetic circular dichroism (XMCD)



# **Magnetization Dynamics on Different Time Scales**

Experimental TR-MOKE result on different time scales



Djordjevic et al., phys. stat. sol. (c) 3, 1347 (2006)

# **Time Scales of Magnetization Dynamics**



- Coherent regime (~10 fs)
- Incoherent "thermalization" dynamics of nonequilibrium electrons (100 fs)
- Quasi-thermal regime: electron temperature, lattice temperature (1 ps)
- Spin-lattice equilibration (100 ps)
- Ultrafast magnetization (spin) dynamics surprising!



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#### **Relevant Facts**



# **Ultrashort Magnetization Dynamics (Theory)**

<u>Question(s)</u> Microscopic mechanism behind the magnetization quenching on ultrashort timescales?

This talk

- 1. Role of coherent effects in the presence of the pulse
- 2. Role of band-structure details
- 3. Role of non-equilibrium electrons
- 4. Role of "true" (correlated) magnetization dynamics
- 5. Role of spin-dependent transport processes
- Answer Probably: "All of the above"
- Agreement Spin-orbit interaction has something to do with it
- <u>Problem</u> Usually "agreement with experiment" for 1-5; BUT dependence on parameters

### (Phenomenological) Three-Temperature Model

 Three systems (electrons, lattice, and spins) in quasi-equilibrium: assign temperatures



from: Kirilyuk et al., Rev. Mod. Phys. **82**, 2731 (2010)

 Separation and quasi-equilibrium assumption OK for picosecond time scale. But:

How to describe ultrafast dynamics in the correlated electron system of the ferromagnet <u>microscopically</u>?

# **Other Approaches**

 $\alpha$ 

- Coherent effects: Important for (few) localized levels with strong spin-orbit coupling
- Landau-Lifshitz-Bloch equations: assume electronic temperature; effective spin-orbit coupling includes spin-fluctuations (around T<sub>c</sub>)



Zhang and Hübner, Phys. Rev. Lett. **85**, 3025 (2000) Bigot, Vomir, Beaurepaire, Nature Phys. **5**, 515 - 520 (2009)

Chubykalo-Fesenko et al, Phys. Rev. B **74**, 094436 (2006) Atxitia, Chubykalo-Fesenko, Walowski, Mann and Münzenberg Phys. Rev. B **81**, 174401 (2010)



 Superdiffusive transport: electrons with different spin leave spot with different velocities
 Battiato, Carva, and Oppeneer, PRL 105, 027203 (2010)

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# **Spin Mixing in Transition Metals**

5

Energy [eV]

-10

W

- Spin mixing important for optical excitation and scattering
- Spin mixing anisotropic ("spin hot-spots")?

Fabian & Das Sarma, Phys. Rev. Lett. 81, 5624 (1998)

- Keep band structure fixed!
- Goal: Obtain quantitative results!

Nickel band structure with "spin hot-spots" 0,8 0,6 0,4 0 0,2 0 -0,2 -0,4 -0,6 -5 -0,8 -1

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#### Elliott-Yafet Mechanism: Spin Relaxation due to Electron-Phonon Scattering

Spin mixing + electron-phonon scattering = spin relaxation

Phonons do <u>not</u> carry angular momentum (spin-diagonal interaction)

Yafet, Solid State Physics, **14** (1963)

Koopmans et al., Nature Mat. **9**, 256 (2010)

#### k-resolved Electron Scattering Dynamics

Equation of motion for electronic dynamics

$$\frac{d}{dt}f^{\mu}(\vec{k}) = \left. \frac{d}{dt}f^{\mu}(\vec{k}) \right|_{e-ph} + \left. \frac{d}{dt}f^{\mu}(\vec{k}) \right|_{opt}$$

carrier distribution in band  $\mu$  with momentum k

Optical excitation of carriers

$$\frac{d}{dt}f^{\mu}(\vec{k})\Big|_{opt} = \frac{2\pi}{\hbar} \sum_{\nu \neq \mu} \left| \vec{d}_{\mu\nu} \cdot \vec{E} \right|^2 \left( f^{\nu}(\vec{k}) - f^{\mu}(\vec{k}) \right) g\left( \left| \epsilon^{\nu}(\vec{k}) - \epsilon^{\mu}(\vec{k}) \right| - \hbar\omega \right)$$

#### k-Resolved Electron-Phonon Scattering

#### Electron-phonon Boltzmann scattering integrals

ab-initio input

$$\begin{aligned} \frac{d}{dt}f^{\mu}(\vec{k}) &= \sum_{\lambda} \sum_{\vec{q}} \left[ w^{\lambda}_{\vec{k}+\vec{q},\mu'\to\vec{k},\mu} f^{\mu'}(\vec{k}+\vec{q}) \left(1-f^{\mu}(\vec{k})\right) - w^{\lambda}_{\vec{k},\mu\to\vec{k}+\vec{q},\mu'} f^{\mu}(\vec{k}) \left(1-f^{\mu'}(\vec{k}+\vec{q})\right) \right] \\ w^{\lambda}_{\vec{k},\mu\to\vec{k}+\vec{q},\mu'} &= \left. \frac{2\pi}{\hbar} \right| \xrightarrow{q} \left[ \tilde{n}^{\vec{q}}_{q} \delta \left( \epsilon^{\mu'}(\vec{k}+\vec{q}) - \epsilon^{\mu}(\vec{k}) - \hbar \omega^{\lambda}_{\vec{q}} \right) \right. \\ &\left. + \left( \tilde{n}^{\lambda}_{-\vec{q}} + 1 \right) \delta \left( \epsilon^{\mu'}(\vec{k}+\vec{q}) - \epsilon^{\mu}(\vec{k}) + \hbar \omega^{\lambda}_{-\vec{q}} \right) \right] \end{aligned}$$

$$\textbf{Two contributions to spin-flip matrix element}$$

 $\xrightarrow{\mathbf{q}} \propto \sum_{\vec{R}} e^{i\vec{q}\cdot\vec{R}} \left\langle \psi_f \left| \vec{\epsilon}_{\vec{q}} \cdot \nabla_{\vec{R}} \left( V + \frac{\hbar}{4m^2c^2} \left( \nabla_{\vec{r}} V \times \vec{p} \right) \cdot \vec{\sigma} \right) \right| \psi_i \right\rangle$ 

S. Essert & H. C. Schneider, Phys. Rev. B **84**, 224405 (2011)

• Band structure @ T = 0K:  $\epsilon^{\mu}(\vec{k})$  • Transition dipole matrix elements  $\vec{d}_{\mu\nu}$ • Phonon dispersion  $\omega_{\vec{q}}^{\lambda}$  • Electron-phonon matrix elements  $M_{\vec{k},\mu;\vec{k}',\mu'}^{\lambda}$ 

#### **Optical Excitation: Dipole Transitions in Nickel**

Dipole transitions with photon energy 1.55 eV in different regions of the Brillouing zone



# **Optical Excitation (2)**



▶ Optical excitation using ultrashort pulse (1.55 eV, 50fs, 4 mJ/cm<sup>-2</sup>)

Demagnetization is not caused by spin mixing during optical excitation

S. Essert & H. C. Schneider, Phys. Rev. B **84**, 224405 (2011)

# **Optical Excitation in Nickel**

- Energy resolved change in carrier occupation
- Optical excitation using ultrashort pulse (1.55 eV, 50fs, 4 mJ/cm<sup>-2</sup>)
- Mainly minority electrons (and holes!) excited



#### **Optical Excitation: Frequency Dependence**

Influence of band structure/spin-mixing on optical excitation



# **Magnetization Dynamics after Optical Excitation**



- Demagnetization mainly due to hole scattering
- Optical excitation and electron-phonon-scattering cannot explain the observed demagnetization
- Other scattering mechanisms?





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#### **Band Structure Properties**



Demagnetization requires energy (delivered by pulse)

Any scattering process = dynamical redistribution of excited carriers

#### How Accurate Can Scattering in a Fixed Band Structure Be?

 Minimal magnetization (maximal demagnetization) by "optimization" for the energy deposited by laser pulse in a fixed band structure

$$\min_{\{n_{\vec{k}}^{\mu}:0\leq n_{\vec{k}}^{\mu}\leq 1\}}\sum_{\vec{k}}\sum_{\mu}n_{\vec{k}}^{\mu}\langle S_{z}\rangle_{\vec{k}}^{\mu}$$

Constraints

$$\sum_{\vec{k}} \sum_{\mu} n_{\vec{k}}^{\mu} = N_{\text{eq}}$$
$$\sum_{\vec{k}} \sum_{\mu} n_{\vec{k}}^{\mu} \epsilon_{\vec{k}}^{\mu} \le E_{\text{eq}} + \Delta E$$

• Deposited energy 
$$\Delta E = \int_{300 \text{ K}}^{T(5 \text{ ps})} dT C_{\text{p}}(T)$$

Essert & Schneider, Phys. Rev. B **84**, 224405 (2011)

# energy (eV)

#### How Accurate Can Scattering in a Fixed Band Structure Be?

 Minimal magnetization (maximal demagnetization) by "optimization" for the energy deposited by laser pulse in a <u>fixed band structure</u>



# **Distribution Functions**

#### after optical excitation minimal magnetization 1,0 1,0 majority-spin majority-spin minority-spin minority-spin equilibrium distribution 0,8 0,8 equilibrium distribution occupation function (Fermi-Dirac-distribution) occupation function (Fermi-Dirac-distribution) 0,6-0,6 0,4 0,4 0,2 0,2 0,0 0,0 -2 -2 0 2 -1 0 2 -1 energy [eV] energy [eV] unlikely to be reached by physical scattering processes agreement with Scattering in DFT band structure in general <u>not</u> sufficient to Carva, Battiato and explain demagnetization Oppeneer, PRL 107 207201 (2011) Exchange splitting change/spin fluctuations must occur on ultrafast timescale in addition to scattering

Rhie et al., Phys. Rev. Lett. **90**, 247201 (2003)

# **Effective Stoner Model (1)**

- Model based on nickel spindependent density of states
- Effective two-band model: Distribution functions  $f_{\downarrow}(E)$  and  $f_{\uparrow}(E)$ spin and energy dependent
- Stoner model with effective Coulomb energy U=5.04 eV
- Exchange splitting

 $\Delta = U_{\rm eff} M = 0.26 \,\rm eV$ 

Density of states

$$\mathcal{D}_{\sigma}(E) = \mathcal{D}_{\sigma}^{(0)}(E \pm \Delta)$$



# **Effective Stoner Model (2)**

- "Realistic" equilibrium magnetization curve
  - $T_{C} = 631 \text{K}$
- Dynamics: Influence of "hot electrons"? ⇒ Include carrier-

carrier and carrier-phonon scattering

 "Non-equilibrium generalization of 3temperature model"



# **Dynamical Stoner Model**

- Boltzmann scattering integrals for carrier-carrier (static Coulomb), carrier-phonon (LA) interaction
- Optical excitation (plasma like)
- Dynamical energy dispersions

scattering integrals: M. Krauß et al, Phys. Rev. B **80**, 180407(R) (2009); dynamical exchange splitting: B. Mueller et al., PRL 111, 167204 (2013)

# **Stoner-Model Demagnetization Dynamics**

- Dynamic exchange splitting "improves" quenching
- Temperature and chemical potential differences contribute to demagnetization dynamics
- Exchange splitting dynamics removes problem with spinflip scattering across a static gap



# **Dynamical Exchange Splitting**



- Electrons heated up by optical exciation  $\mu_{\uparrow} \neq \mu_{\downarrow}$
- Scattering equilibrates chemical potentials  $\mu_{\uparrow}, \mu_{\downarrow} \rightarrow \mu$
- Dynamical exchange splitting shifts bands: changes quasiequilibrium chemical potential µ



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#### Ferromagnet Lifetimes + "History"

- So far: measurement and calculation of demagnetisation dynamics fraught with inaccuracies
- Simpler(?) problem: Measure/calculate lifetimes
- Theory developed for electron gas in the 1950s and 1960 by Ritchie, Quinn & Ferrell, Ritchie, Quinn (see, e.g., Mahan: Many-particle physics)
- Surface states by Echenique, Chulkov and coworkers
- DFT + Many-Particle Theory community (Ambrosch-Draxl, Godby, Louie, Chulkov & Echenique)



# **Lifetimes: Theory**

Evaluate dielectric function

$$\varepsilon(\vec{q},\omega) = 1 - V_q \sum_{\mu\nu\vec{k}} |B_{\vec{k}\vec{q}}^{\mu\nu}|^2 \frac{f_{\vec{k}}^{\nu} - f_{\vec{k}+\vec{q}}^{\mu}}{\hbar\omega + \epsilon_{\vec{k}}^{\nu} - \epsilon_{\vec{k}+\vec{q}}^{\mu} + i\hbar\gamma}$$

• with wave function overlap  $B_{\vec{k}\vec{q}}^{\mu\nu} = \langle \psi_{\vec{k}+\vec{q}}^{\mu} | e^{i\vec{q}\cdot\vec{r}} | \psi_{\vec{k}}^{\nu} \rangle$ 

• spin-mixing (spin-orbit) coupling included  $|\psi_{\vec{k}}^{\mu}\rangle = a_{\vec{k}}^{\mu}|\uparrow\rangle + b_{\vec{k}}^{\mu}|\downarrow\rangle$ 

• Coulomb pot. 
$$V_q = \frac{e^2}{\varepsilon_0 q^2}$$

Use q-dependent tetrahedron method (implemented by S. Kaltenborn)

- DFT code including spin-orbit coupling: ELK
- No local-field effects

#### **Lifetimes: Theory**

- Lifetimes from Fermi's Golden Rule, i.e., G<sub>0</sub>W<sub>0</sub> approximation for self-energy
- momentum and band dependent rate:  $(v, \vec{k}) \rightarrow (\mu, \vec{k} + \vec{q})$

$$\gamma_{\vec{k}}^{\nu} = \frac{2}{\hbar} \sum_{\mu \vec{q}} \frac{\Delta q^3}{(2\pi)^3} V_q \left[ B_{\vec{k}\vec{q}}^{\mu\nu} \right]^2 f_{\vec{k}+\vec{q}}^{\mu} \frac{\operatorname{Im} \varepsilon(\vec{q}, \Delta E)}{|\varepsilon(\vec{q}, \Delta E)|^2}$$

- energy difference  $\Delta E = \epsilon^{\mu}_{\vec{k}+\vec{q}} \epsilon^{\nu}_{\vec{k}}$
- again, spin-orbit coupling included  $|\psi_{\vec{k}}^{\mu}\rangle = a_{\vec{k}}^{\mu}|\uparrow\rangle + b_{\vec{k}}^{\mu}|\downarrow\rangle$

#### **Spin-dependent Lifetimes in Ferromagnets**

- Success explaining spinintegrated lifetimes
- Problems with spin dependence
- Reason: Singlet vs. triplet scattering??
- Discrepancy with calculations; see also Goris et al., Phys. Rev. Lett. 107, 026601 (2011)



Knorren, Bennemann, Burgermeister, Aeschlimann, Phys. Rev. B 61, 9427 (2000)

# **Spin-dependent Lifetimes in Ferromagnets**

- GW calculations predict essentially results from random-k model (DOS!)
- T-matrix yields only small differences





Zhukov, Chulkov, Echenique, Phys. Rev. Lett. 93, 096401 (2004); Phys. Rev. B 73, 125105 (2006)

# Iron vs. Nickel: DOS/random-k



- Very different DOS at Fermi energy for Fe and Ni
- High spin polarisation at Fermi energy: very different scattering phase space in the different spin channels
- Random-k model: spin-dependent DOS determines lifetimes

# **Cobalt DOS**



 Pronounced spin polarisation at Fermi energy



# Lifetimes in Iron

- Compute k- and band resolved lifetimes
- Average lifetimes in energy "bins"
- Use scatter in k as "error bar"
- Small error bar: Only few bands intersect Fermi energy
- Good agreement for "spin asymmetry"
- Results essentially in agreement with earlier abinitio calculations
- "Spin-integrated" lifetimes also in agreement with experiment\*

Knorren, Bennemann, Burgermeister, Aeschlimann, Phys. Rev. B 61, 9427 (2000)

Kaltenborn and Schneider, arXiv1403.4728(2014)



# **Spin-dependent Lifetimes in Cobalt**

- Pronounced scatter
- Good agreement with experiment for "spin asymmetry"
- "Spin-integrated" lifetimes also in agreement with experiment\*
- Spin-orbit coupling "flips spins"; DOS argument for separate spin channels does not apply

Kaltenborn and Schneider, arXiv1403.4728(2014)



Goris et al., Phys. Rev. Lett. 107, 026601 (2011)

# **Lifetimes in Nickel**

- Small "error bar" (scatter in k)
- Good agreement with measurements
- Very different result from earlier calculations without spin-orbit coupling
- Spin-orbit coupling "flips spins"; DOS argument for separate spin channels does not apply



Knorren, Bennemann, Burgermeister, Aeschlimann, Phys. Rev. B 61, 9427 (2000)

Kaltenborn and Schneider, arXiv1403.4728(2014)

# **Electronic Lifetime in Aluminum**



- Benchmark results for aluminium calculated with Wien97, LMTO codes without spin-orbit coupling in wave functions
- Surprisingly large effect due to inclusion of spin-orbit coupling in wave functions
   Kaltenborn and Schneider, arXiv1403.4728(2014)

#### Heusler Alloys: Half-Metallic Ferromagnets

Spin polarization: 
$$P(E) = \frac{N(E_{\uparrow}) - N(E_{\downarrow})}{N(E_{\uparrow}) + N(E_{\downarrow})}$$



#### **Heusler Compounds**



Compare CoMnSi and CoFeSi

 Gap below and above Fermi energy for minority electrons Band structure calculation checked against: B. Balke et al., Phys. Rev. B 74, 104405 (2006)

# Heuslers: Spin-dependent Lifetimes

- Small spin-asymmetry (minority/majority) over wide energy range
- Gap in minority DOS not visible
- Only around special energies a ratio of 4 or 5 to 1 is reached



Kaltenborn and Schneider, Phys. Rev. B 89, 115127 (2014).

# Conclusions

- Ab-initio based calculation of optical excitation and "classical" Elliott-Yafet carrier-spin dynamics in ferromagnetic metals
- DFT (T = 0K) band structure and electron-phonon coupling matrix elements
- "Simple" model including dynamics of exchange splitting (magnetic order parameter) improves achievable magnetization quenching at realistic fluences
- Calculation of spin asymmetry including spin-orbit coupling in the wave functions for ferromagnets and Heusler compounds
- Spin-orbit coupling washes out differences in the scattering phase space in the spin-dependent DOS