

Skyrmion dynamics in nanostructures

Oscillators and propagation in disordered systems

Joo-Von Kim

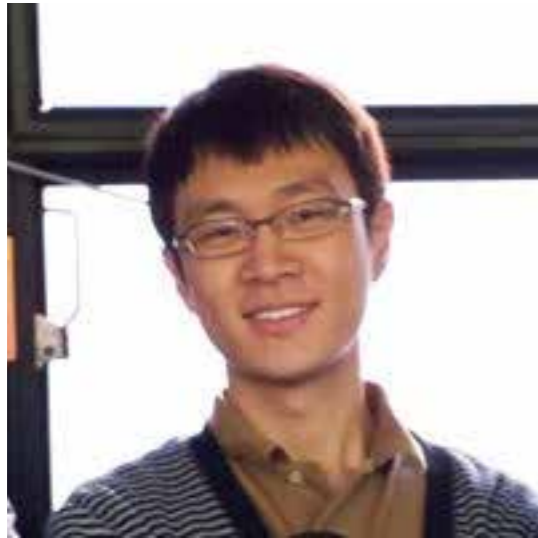
Centre for Nanoscience and Nanotechnology (C2N)

CNRS, Univ. Paris-Sud, Université Paris-Saclay – Orsay, France



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Acknowledgements



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Centre for Nanoscience and Nanotechnology (C2N)



Merger between the *Institut d'Electronique Fondamentale* (Orsay) and the *Laboratoire de Photonique et de Nanostructures* (Marcoussis), 1 June 2016



**Saclay plateau
end of 2017**

- > 400 personnel, 18 000 m² with 2 800 m² of clean room
- Photonics | Materials | Nanoelectronics | Microsystems & Nanobiofluidics

« Mariage pluvieux, mariage heureux ? »



The Orsay campus on
1 June 2016 ...

Emmanuelle Louis
@E_LouisUPSud

Following

Inondations campus d'Orsay - vallée @u_psud -

[View translation](#)

RETWEETS 15 LIKES 4

9:13 AM - 1 Jun 2016

The new building at the start of 2017 ...





- Brief overview of skyrmions in ultrathin ferromagnets
- Skyrmion oscillators
- Current-driven motion in disordered systems
- Summary and outlook

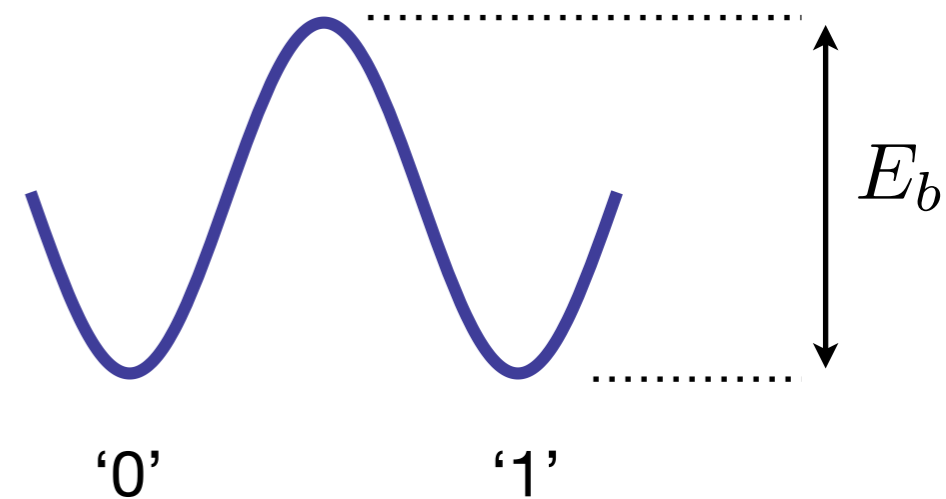
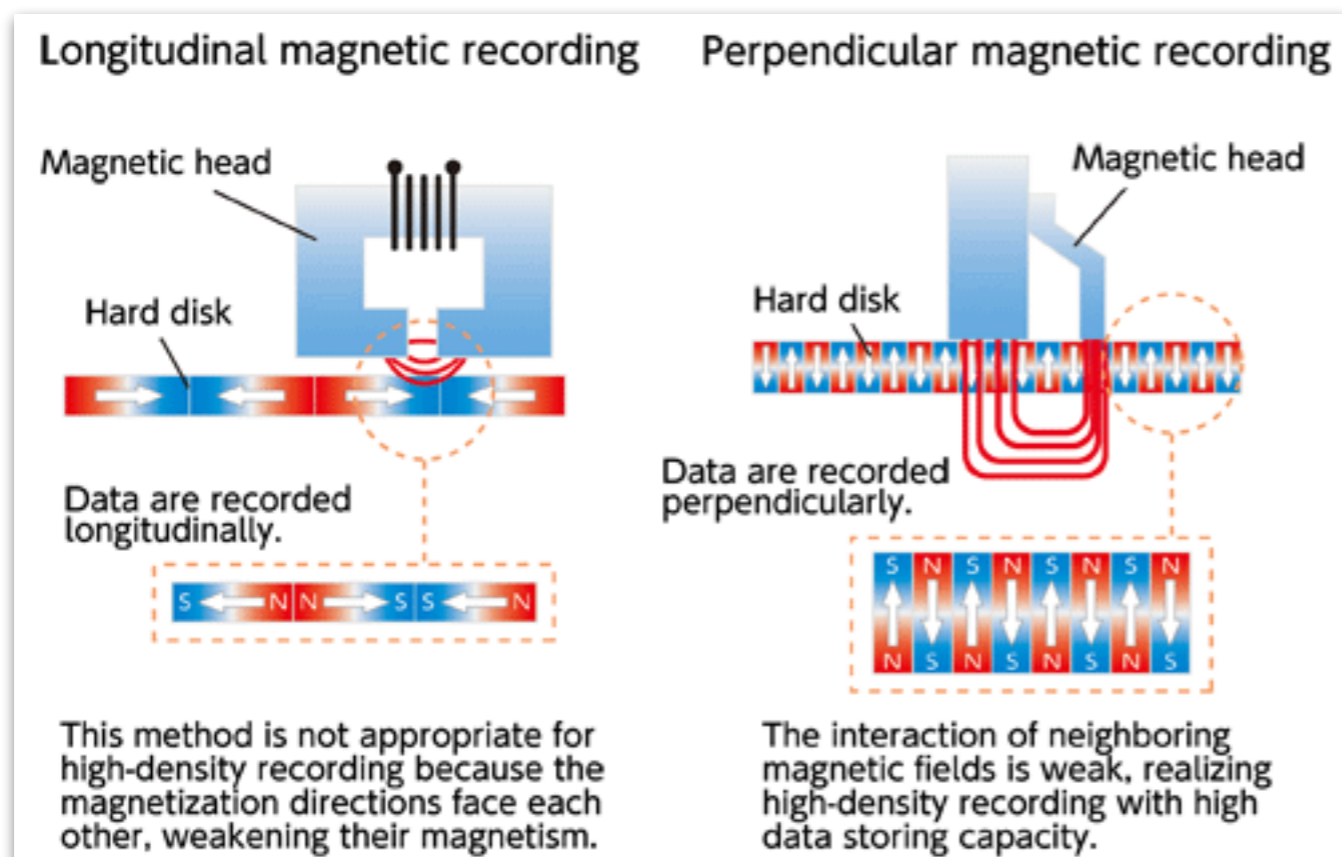
Ultrathin metallic ferromagnets



- Ultrathin metallic ferromagnets, such as Co and its alloys, are interesting for spintronics applications
 - Strong ferromagnet, even above room temperature
 - Strong perpendicular magnetic anisotropy (PMA)

Narrower domain walls =
higher information storage
density

Larger energy barriers =
higher thermal stability

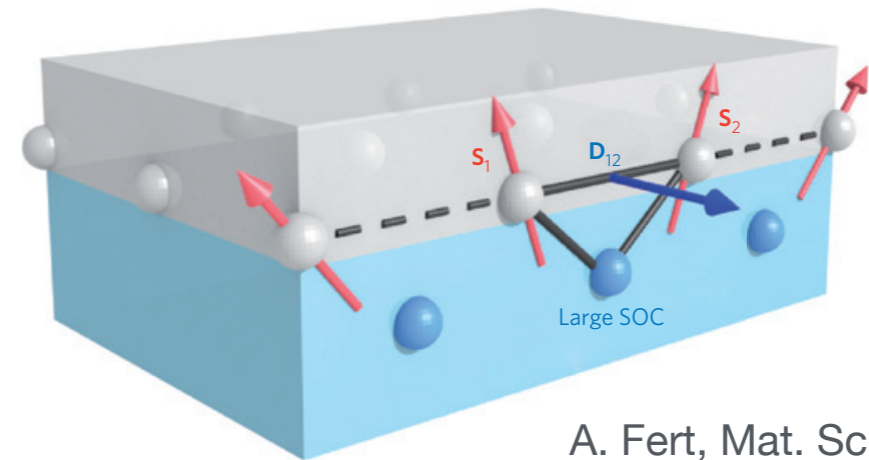


Interface-driven chiral interactions



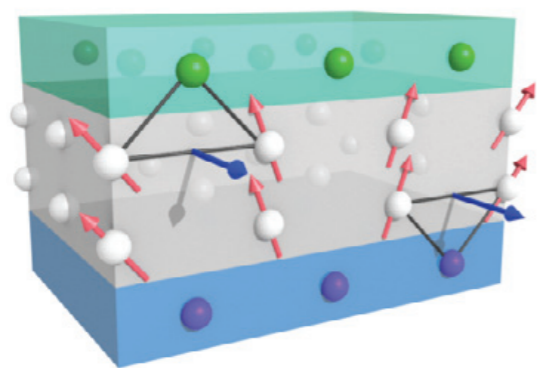
- Strong spin-orbit coupling at interfaces induces chiral (Dzyaloshinskii-Moriya) interactions

$$\mathcal{H}_{\text{DM}} = -\vec{D}_{12} \cdot (\vec{S}_1 \times \vec{S}_2)$$



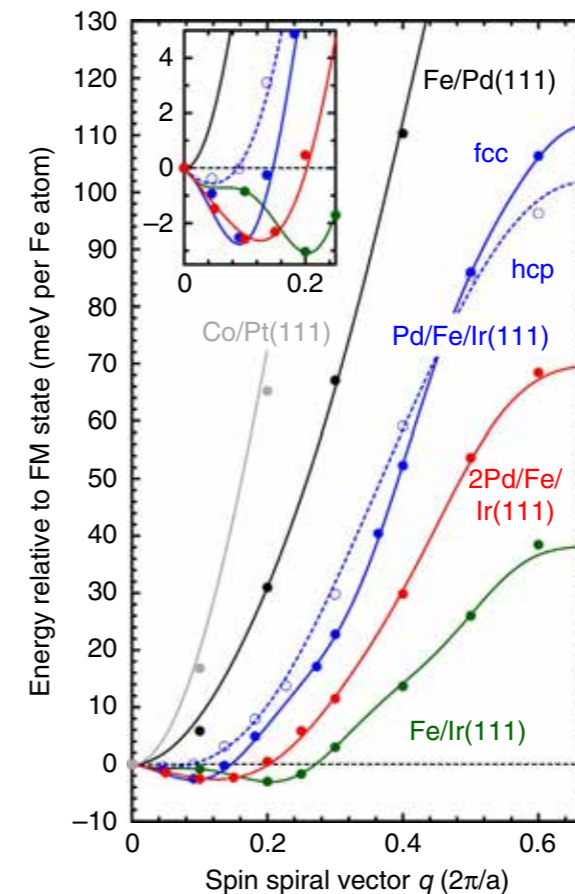
A. Fert, Mat. Sci. Forum (1990)
A. Fert and P. M. Levy, PRL (1980)

- DMI can be tailored through choice of multilayer configuration and materials



Pt/Co/Ir ...

C. Moreau-Luchaire *et al.*,
Nat. Nanotechnol. (2016)

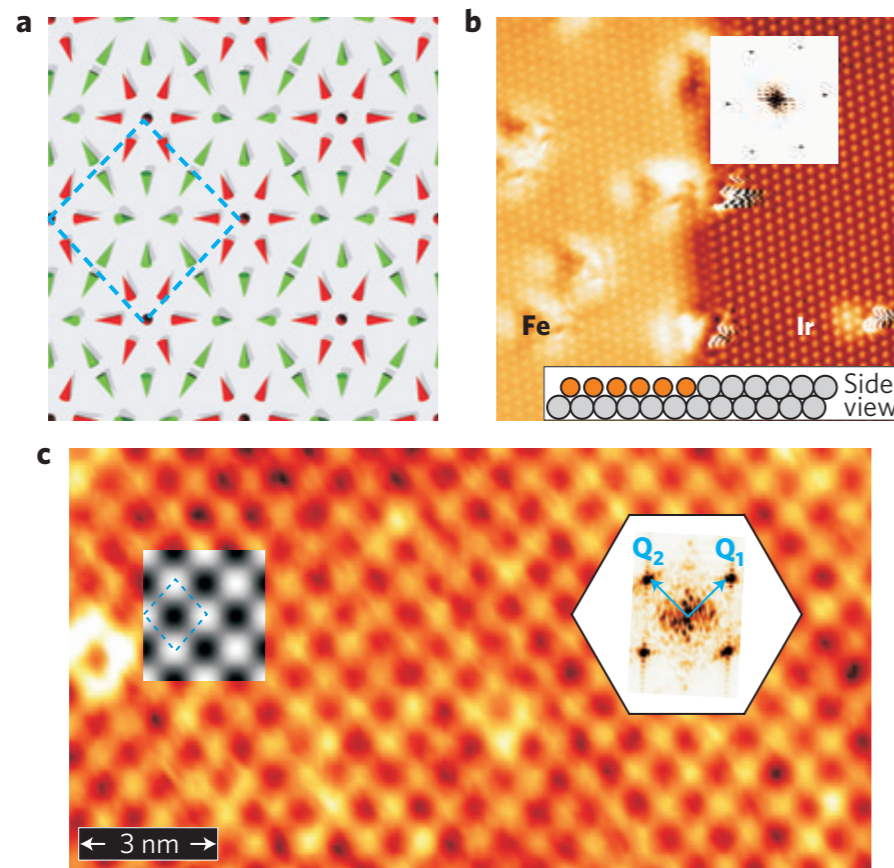


B. Dupé *et al.*,
Nat. Commun. (2014)



Spontaneous atomic-scale magnetic skyrmion lattice in two dimensions

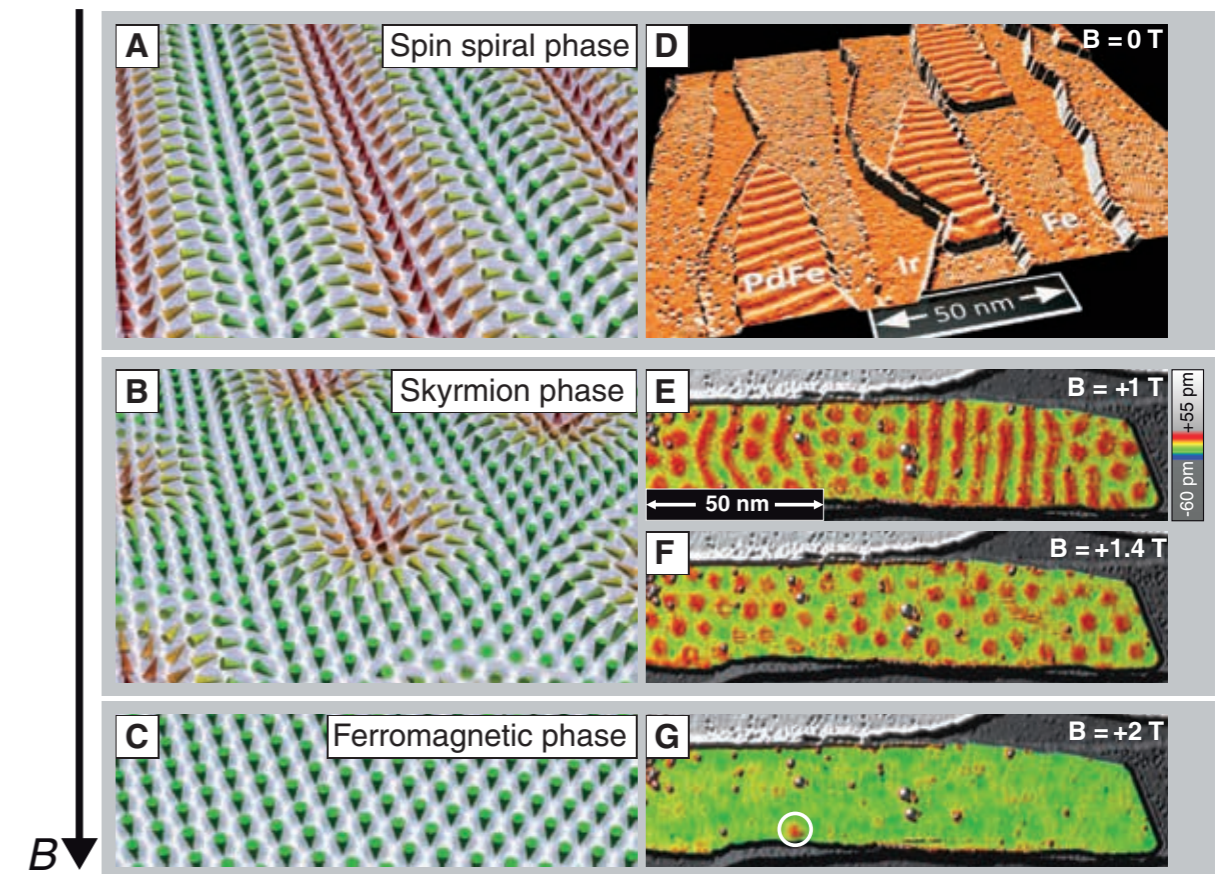
Stefan Heinze^{1*}, Kirsten von Bergmann^{2*}, Matthias Menzel^{2†}, Jens Brede², André Kubetzka², Roland Wiesendanger², Gustav Bihlmayer^{3†} and Stefan Blügel³



Nano-skyrmion lattice in monolayer Fe/Ir(111)

Writing and Deleting Single Magnetic Skyrmions

Niklas Romming, Christian Hanneken, Matthias Menzel, Jessica E. Bickel,* Boris Wolter, Kirsten von Bergmann,† André Kubetzka,† Roland Wiesendanger

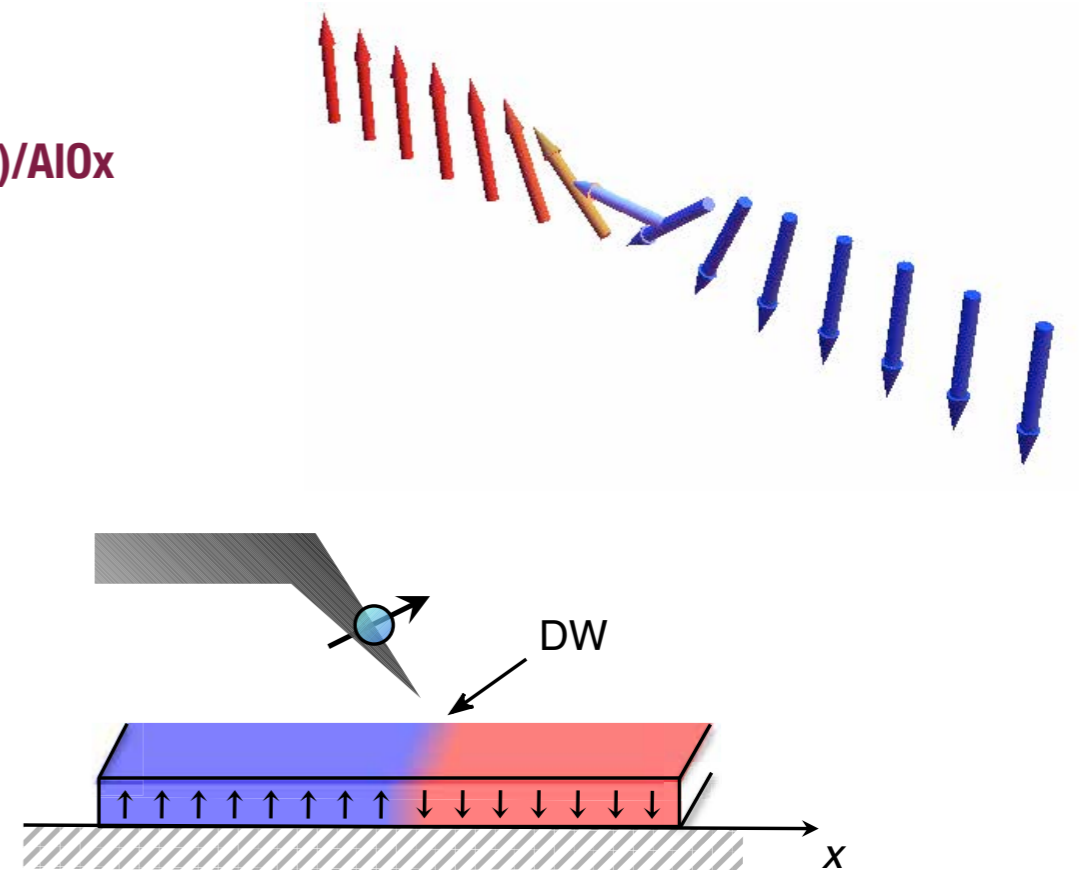
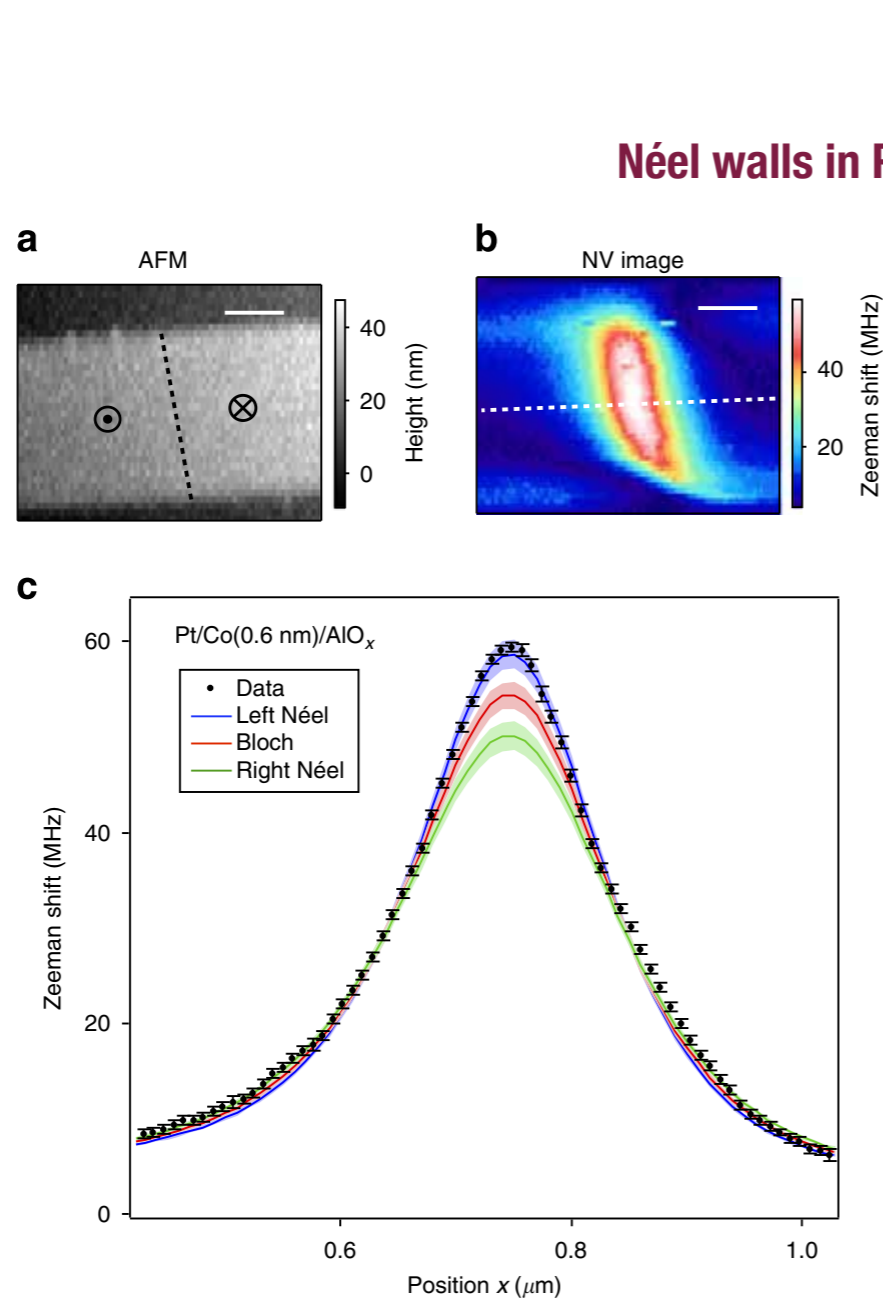


Pd/Fe/Ir(111)

Chiral magnetic states in ultrathin ferromagnets



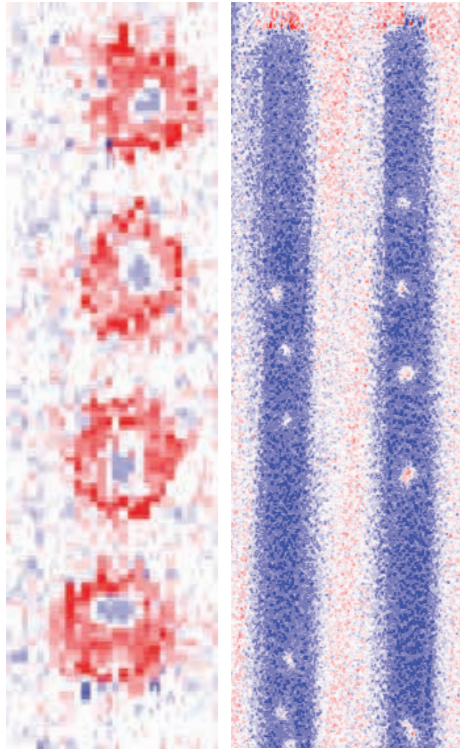
- Perpendicular anisotropy systems with interfacial DMI can support **Néel domain walls and skyrmions**



J.-P. Tétienne *et al.*, Nat. Commun. (2015)

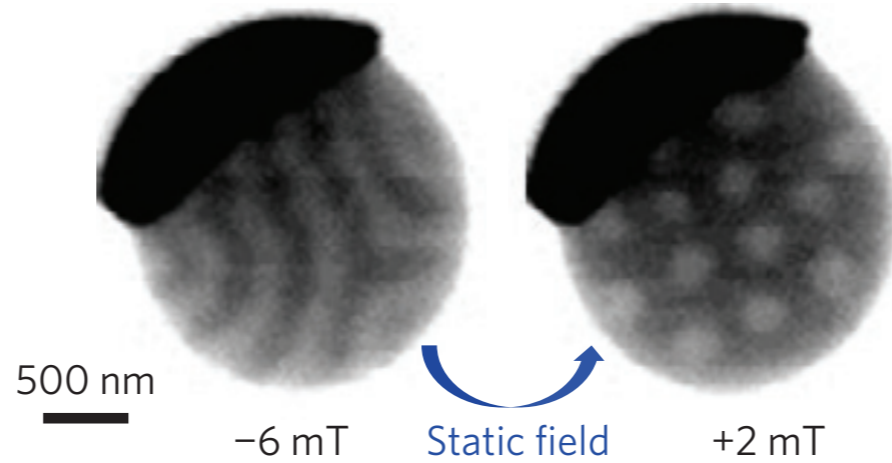
Skyrmions in [Ir/Co (0.6 nm)/Pt]_n

300 nm disks
200 nm tracks



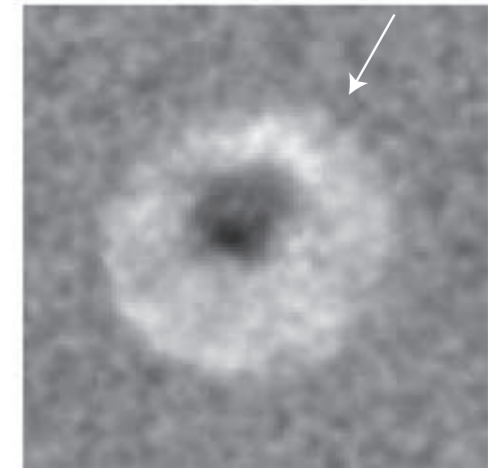
C. Moreau-Luchaire *et al.*, Nat. Nanotechnol. (2016)

Skyrmions in Pt/Co (0.9 nm)/Ta



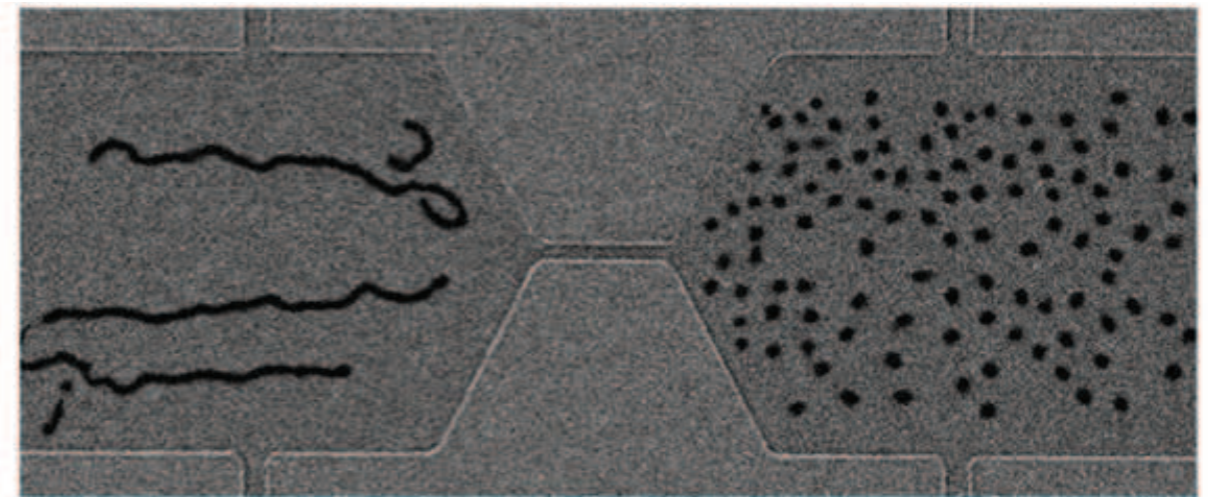
S. Woo *et al.*, Nat. Mater. (2016)

Skyrmions in Pt/Co (1 nm)/MgO



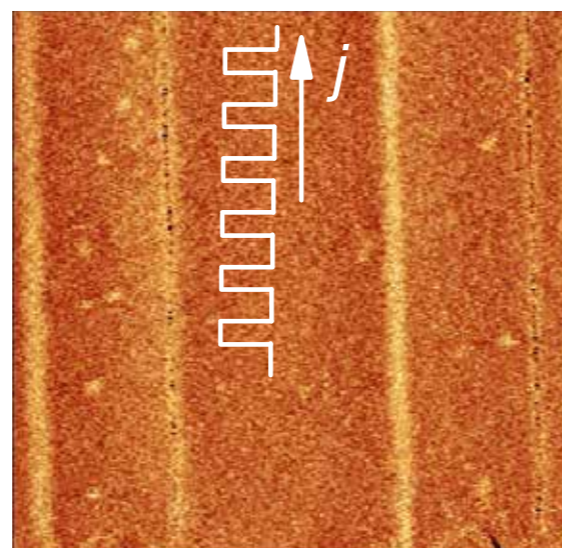
O. Boulle *et al.*, Nat. Mater. (2016)

Skyrmionic bubbles in Ta/CoFeB (1.1 nm)/TaOx



W. Jiang *et al.*, Science (2015)

Skyrmions in Pt/(Ni/Co/Ni)/Au/(Ni/Co/Ni)/Pt

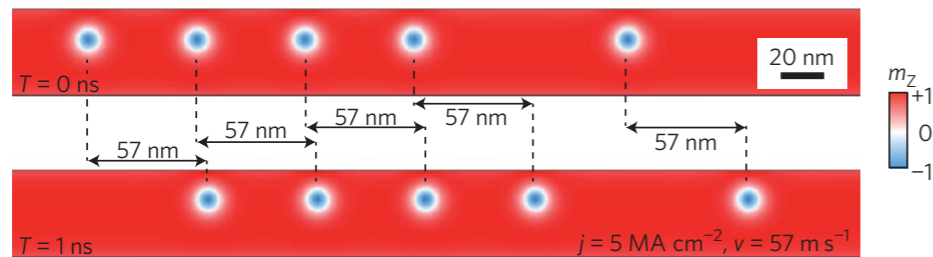


A. Hrabec *et al.*, arXiv:1611.00647

Potential applications of skyrmions

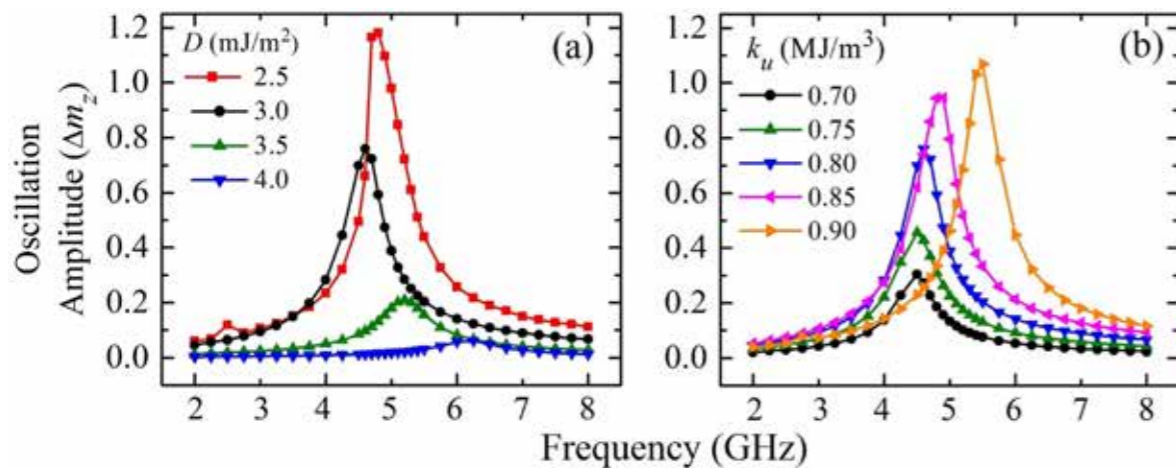


Racetrack memory



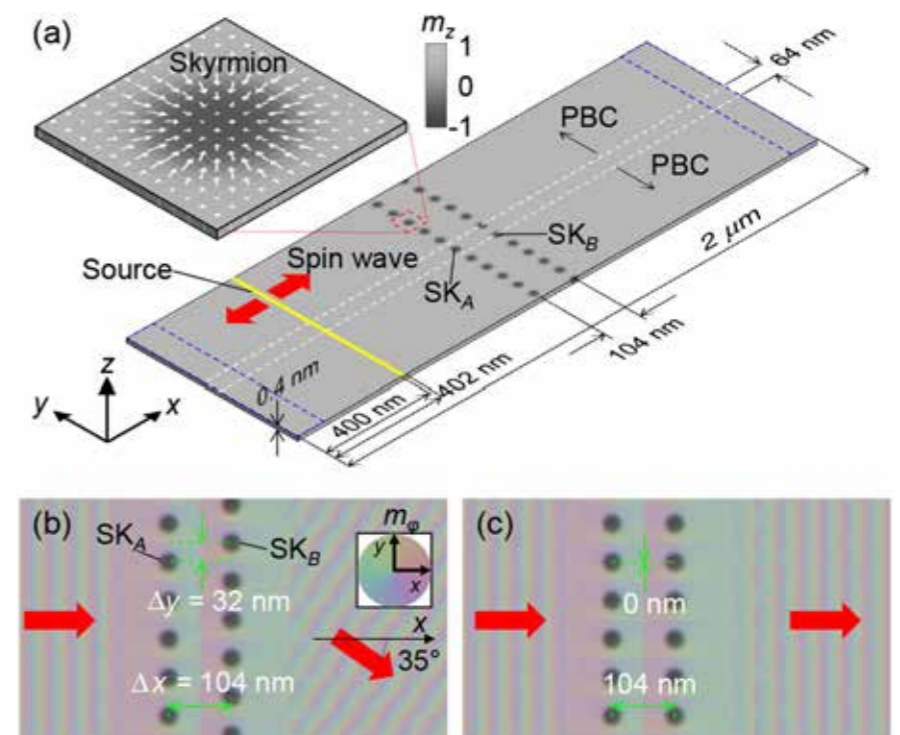
J. Sampaio *et al.*, Nat. Nanotechnol. (2013)

Microwave detection and energy harvesting



G. Finocchio *et al.*, Appl. Phys. Lett. (2015)

Spin wave refraction



K.-W. Moon *et al.*, Phys. Rev. Applied (2016)

Oscillators, logic gates, ...

Exploit linear and/or gyrotropic motion in one way or another



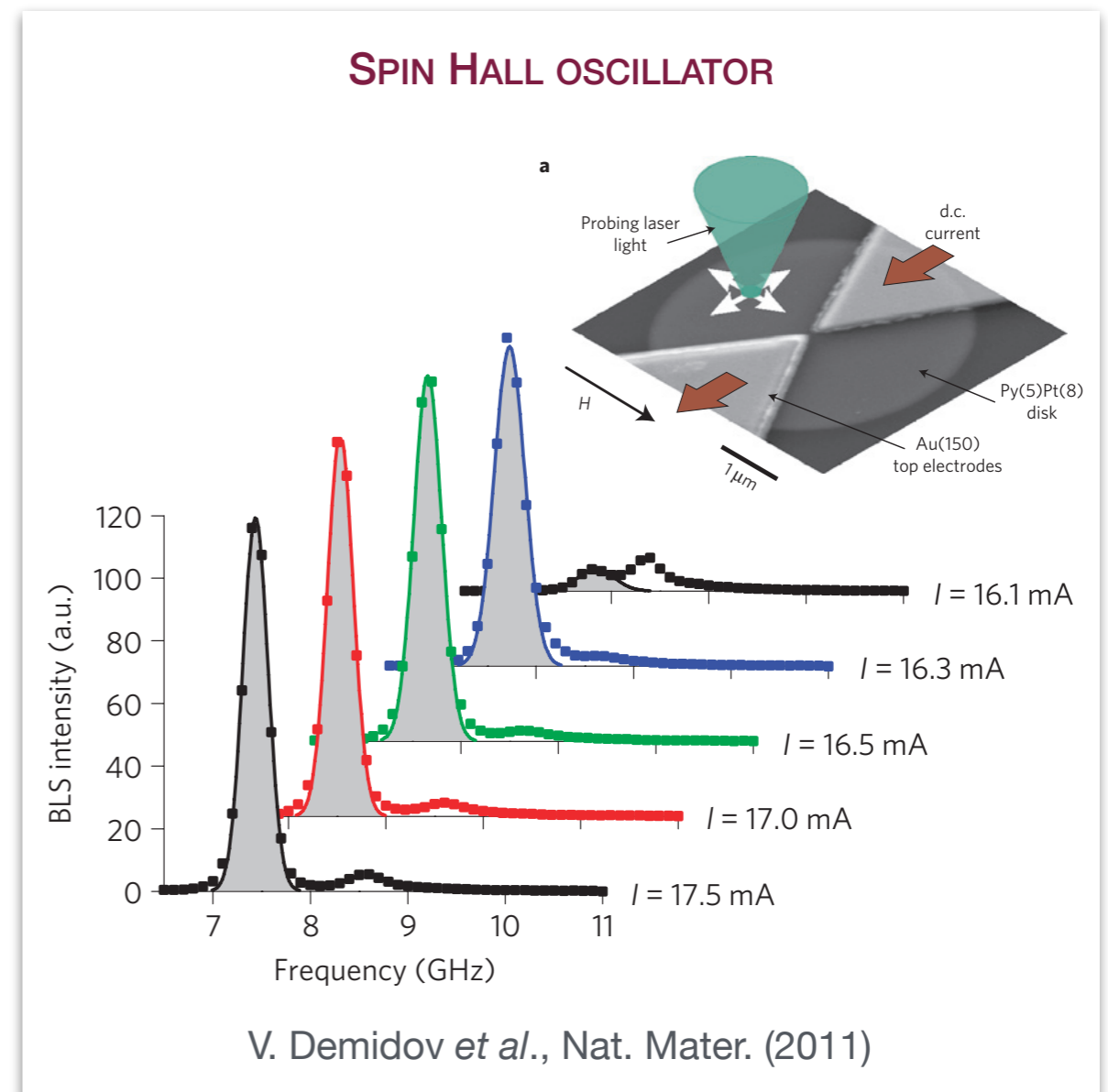
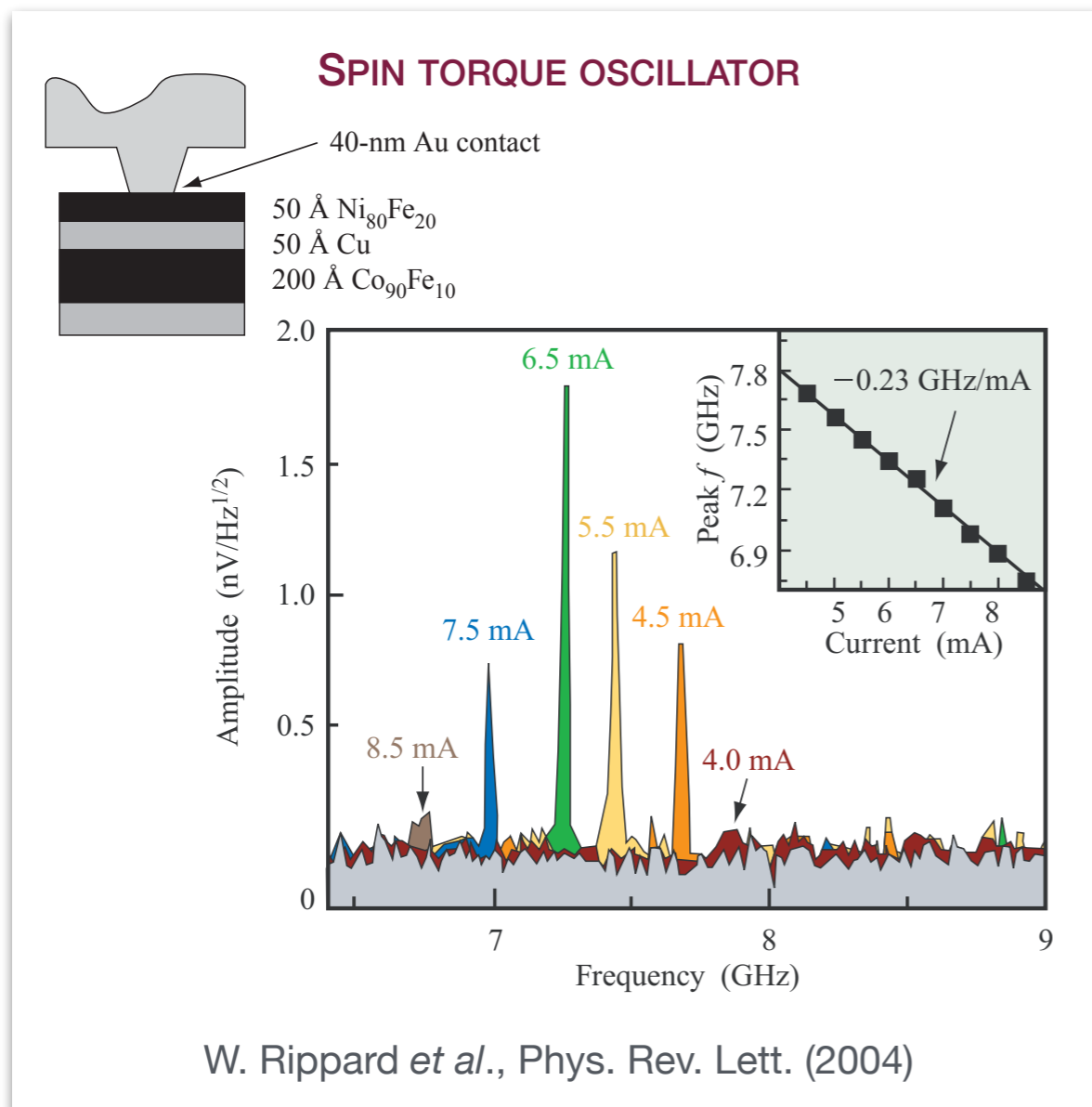
- Brief overview of skyrmions in ultrathin ferromagnets
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- Current-driven motion in disordered systems
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Spin-torque nano-oscillators (STNO)



Current-induced spin torques allow for nonlinear dynamical phenomena not accessible with magnetic fields alone

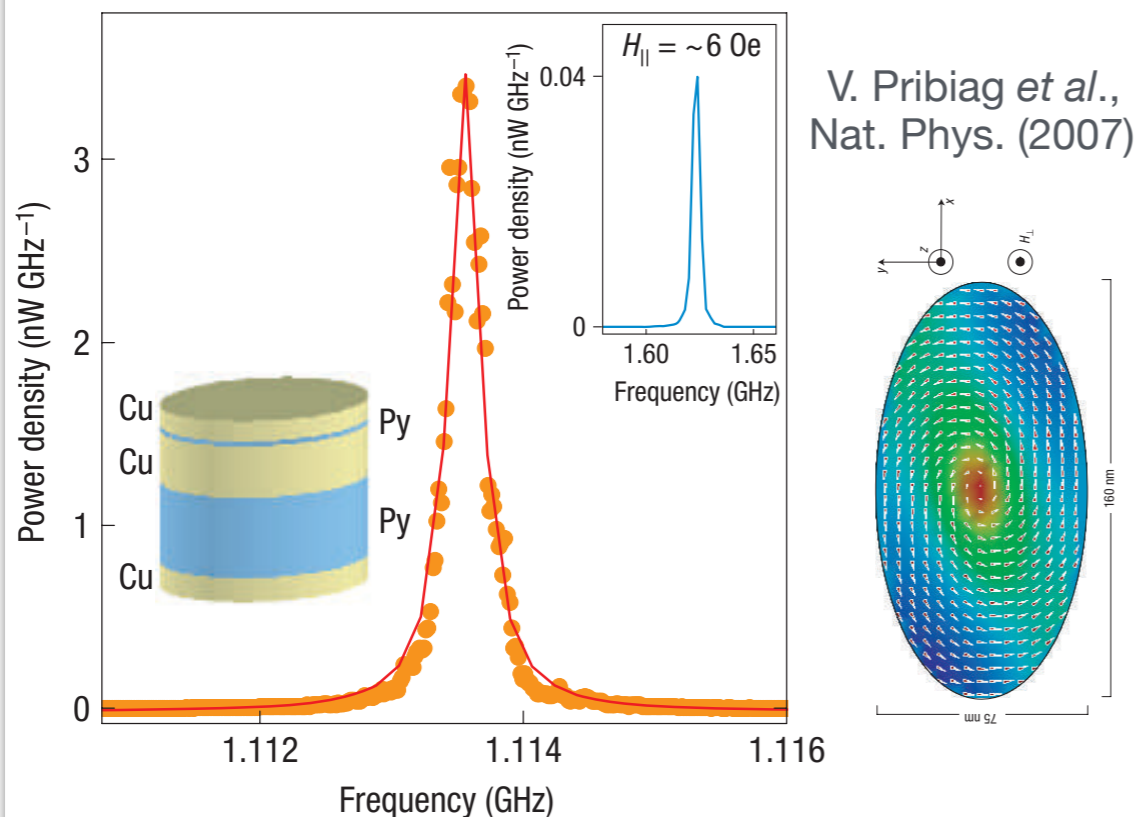
Example: *self-sustained magnetization oscillations*





In STNOs based on solitons such as vortices, the magnetostatic or Zeeman energy defines a *confinement* potential, i.e. gyration/oscillation frequencies.

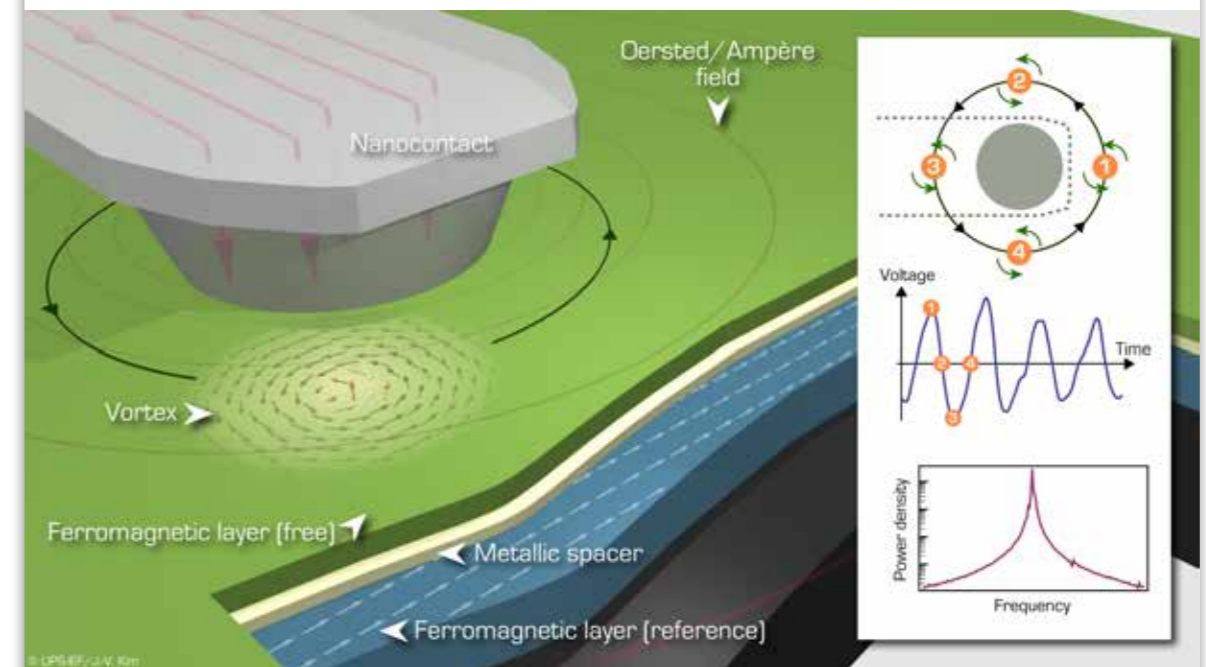
NANOPILLARS: MAGNETOSTATICS



$$U(\|\vec{X}\|) = \frac{1}{2}\kappa\|\vec{X}\|^2 + \dots$$

B. Ivanov & C. E. Zaspel, Phys. Rev. Lett. (2007)

NANOCONTACTS: OERSTED FIELDS



$$U(\|\vec{X}\|) = \kappa\|\vec{X}\| + \dots$$

Q. Mistral, JVK *et al.*, Phys. Rev. Lett. (2008)



- Magnetization dynamics governed by Landau-Lifshitz equation

$$\frac{d\mathbf{m}}{dt} = \underbrace{-\gamma_0 \mathbf{m} \times \mathbf{H}_{\text{eff}}}_{\text{Precession}} + \underbrace{\alpha \mathbf{m} \times \frac{d\mathbf{m}}{dt}}_{\text{Damping}} + \underbrace{\boldsymbol{\Gamma}_{\text{ST}}}_{\text{Spin torques}}$$

- By assuming profile for vortex/skyrmion core, can integrate out degrees of freedom and describe dynamics in terms of core position

$$\underbrace{\mathbf{G} \times \dot{\mathbf{X}}_0}_{\text{Gyrotropic}} + \underbrace{\alpha D \dot{\mathbf{X}}_0}_{\text{Damping}} = - \underbrace{\frac{\partial U}{\partial \mathbf{X}_0}}_{\text{Potential force}} + \underbrace{\mathbf{F}_{\text{ST}}}_{\text{Spin torques}}$$

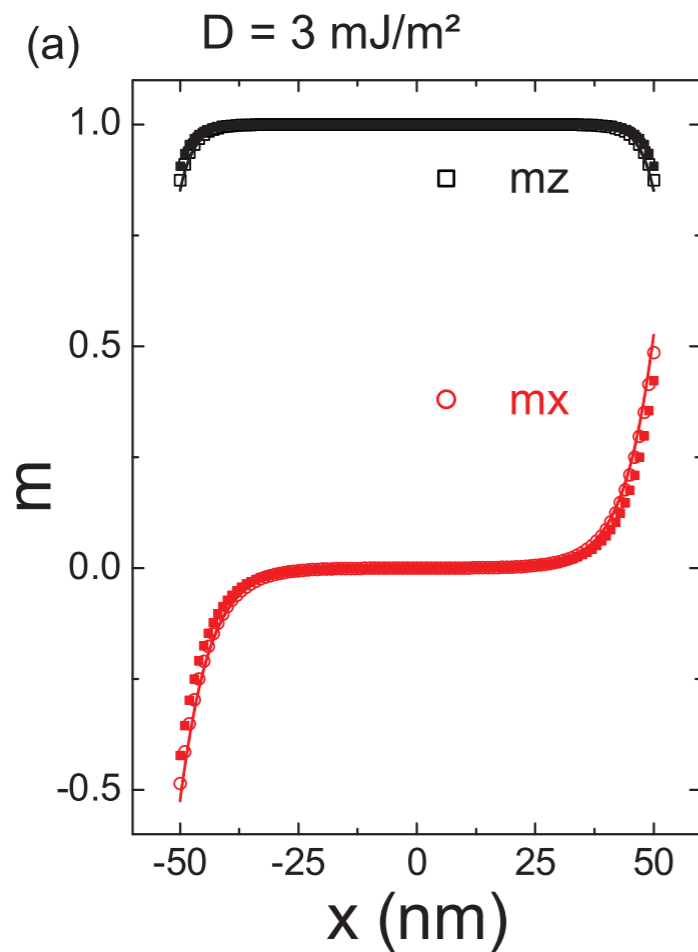
- When **spin torques compensate damping**, self-sustained gyration occurs
 → *spin-torque oscillator*

Skyrmion oscillators?

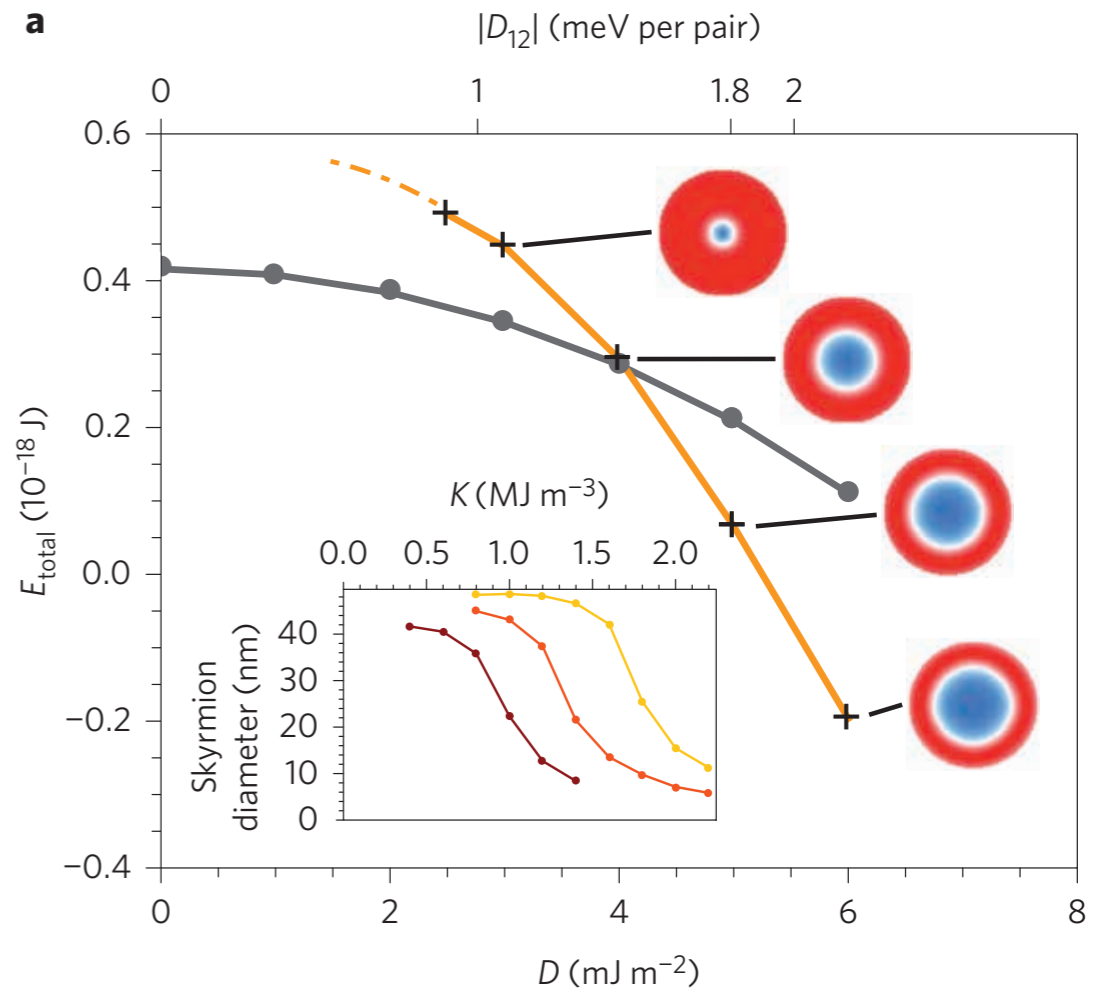


Is there a confinement potential for skyrmions?

Yes! Boundaries provide natural confinement due to repulsion with *partial walls* at edges.



S. Rohart & A. Thiaville, Phys. Rev. B (2013)

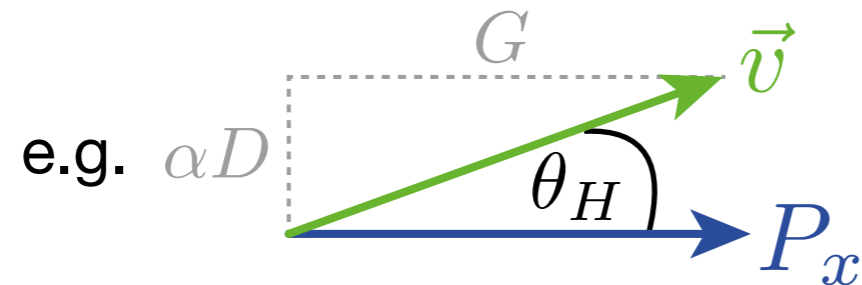


A. Fert *et al.*, Nat. Nanotech. (2013)
J. Sampaio *et al.*, Nat. Nanotech. (2013)

CPP torques with inhomogeneous polarizer



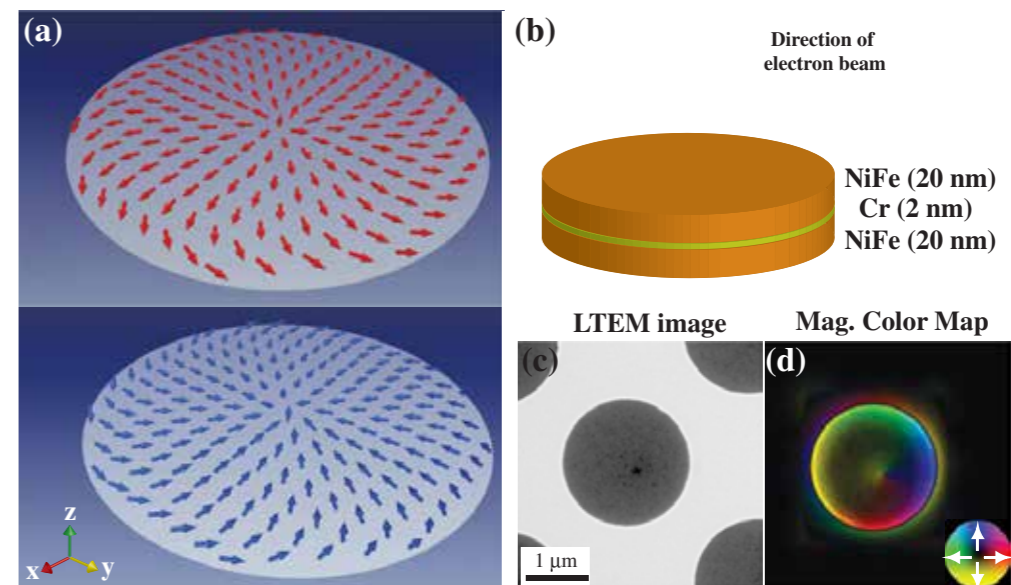
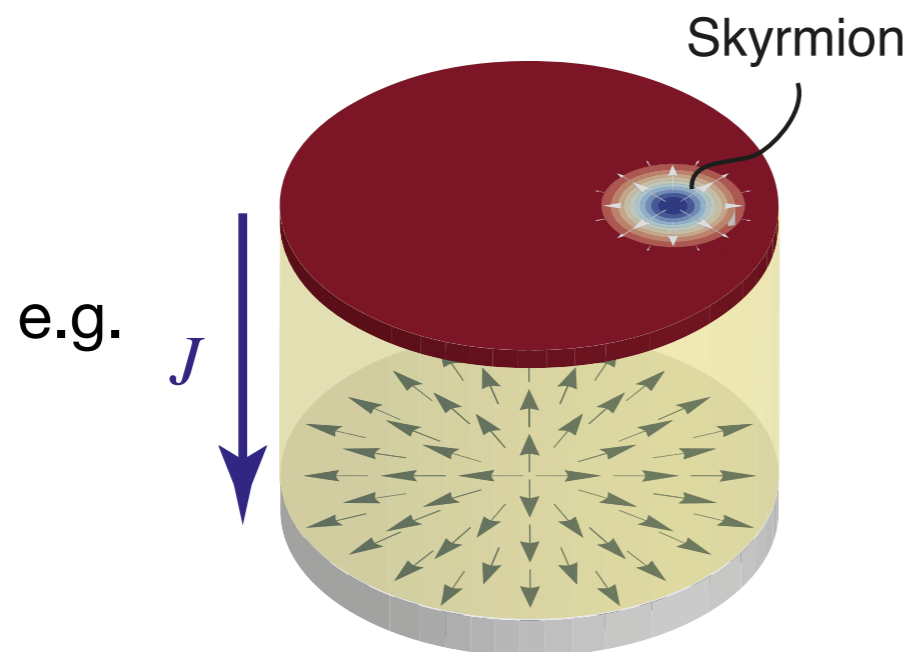
- Under CPP Slonczewski torques (\sim SHE), skyrmion motion is not collinear with spin polarization vector P



$$\tan \theta_H = \frac{\alpha D}{G}$$

Deflection analogous to Hall effect

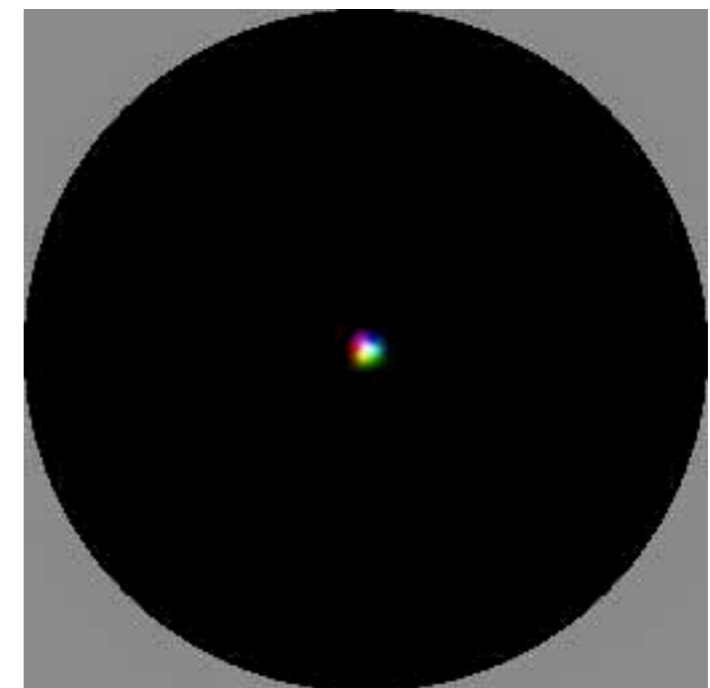
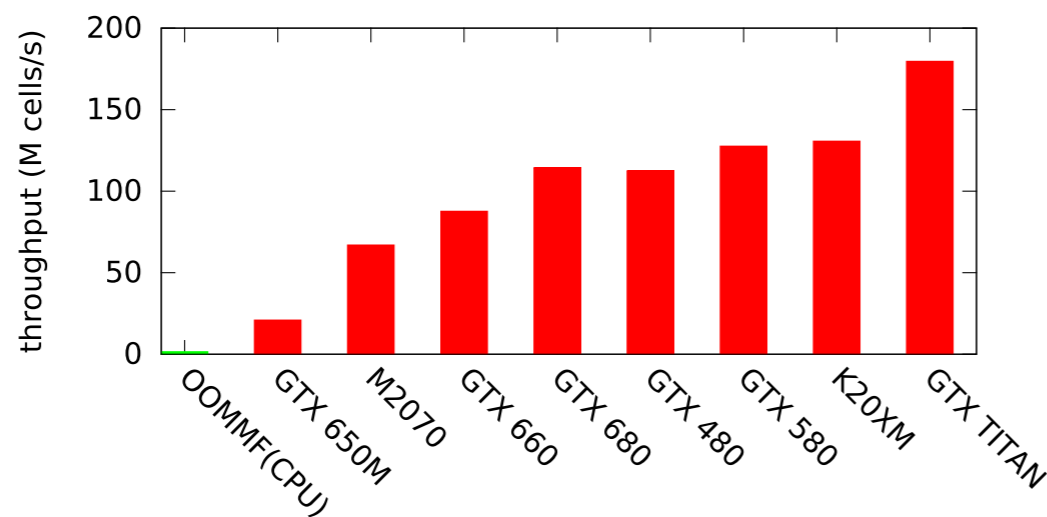
- Could a vortex-like polarizer, combined with edge confinement, lead to skyrmion oscillations?



C. Phatak *et al.*, Phys. Rev. Lett. (2012)

- Performed micromagnetics simulations using MuMax3 code
 - Solves Landau-Lifshitz-Gilbert + spin torques using finite difference method
 - Graphics processing units (GPUs) for fast computation of dipole-dipole interaction
 - Standard energy terms: exchange, anisotropy, dipole-dipole, DMI, Zeeman

$$\frac{d\mathbf{m}}{dt} = -\gamma_0 \mathbf{m} \times \mathbf{H}_{\text{eff}} + \alpha \mathbf{m} \times \frac{d\mathbf{m}}{dt} + \mathbf{\Gamma}_{\text{ST}}$$



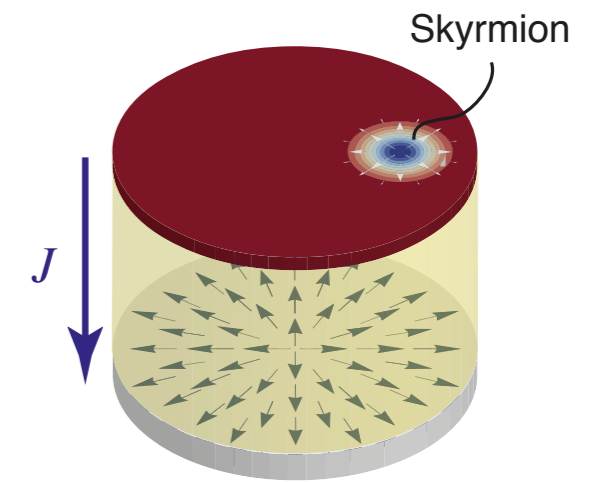
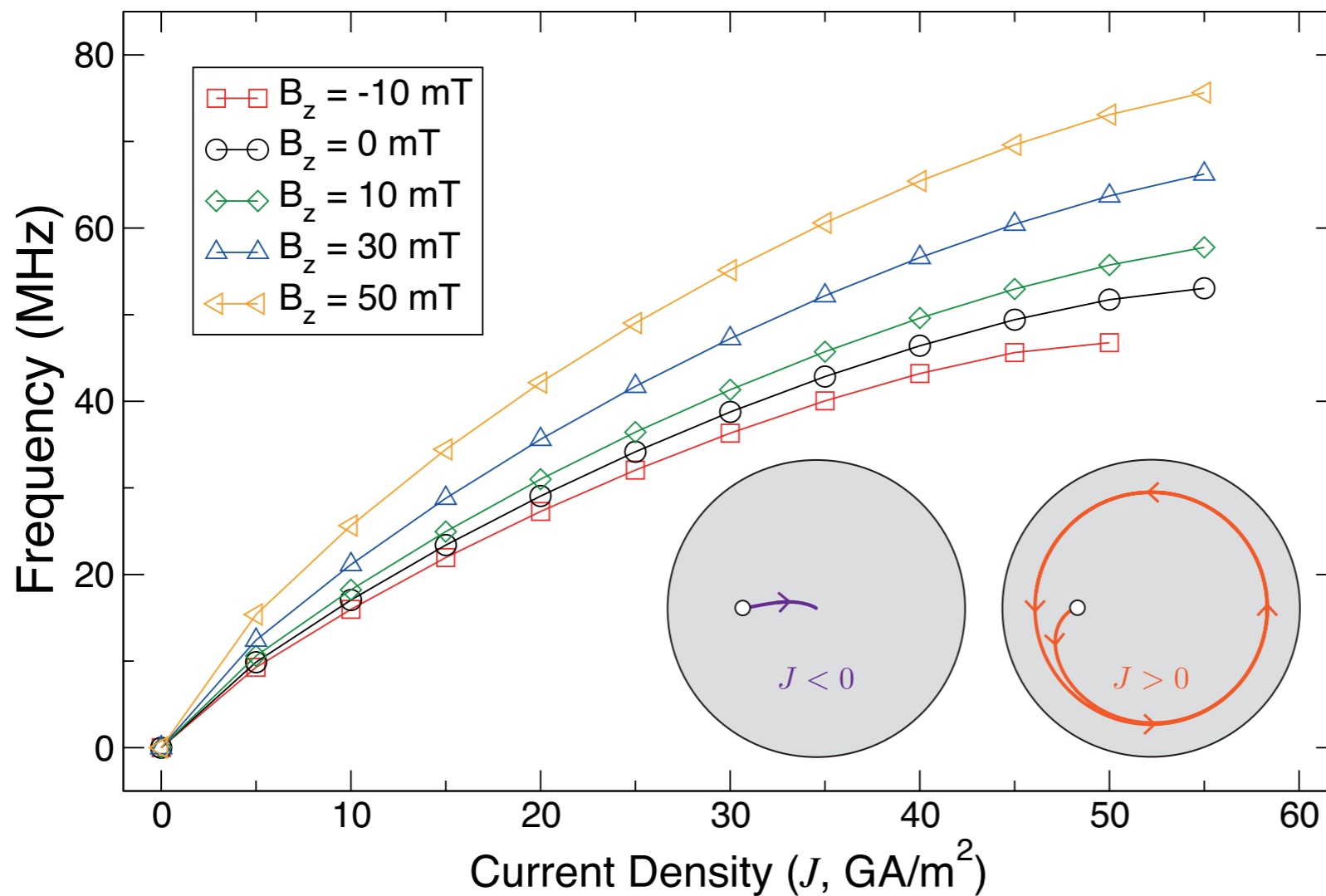
A. Vansteenkiste *et al.*, AIP Adv. (2014)

Radial polarizer – MuMax simulations

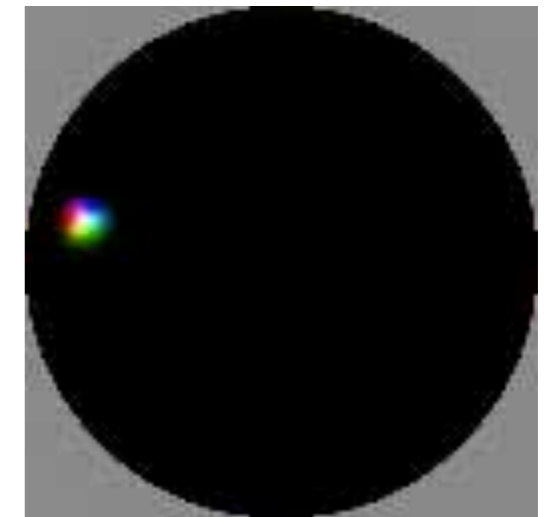
F. Garcia-Sanchez *et al.*, New J. Phys. (2016)



Oscillations occur for only one current polarity
("outward" motion)



150 nm / 128 cells



Parameters based on
Pt/Co (0.6 nm)/AlOx
[M. Belmeguenai *et al.*, PRB 2015]

$$\alpha = 0.3, \theta_H \approx 20^\circ$$

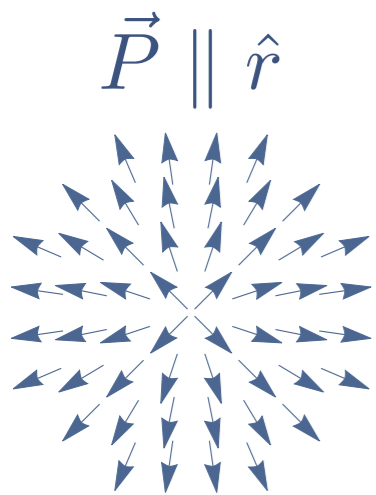
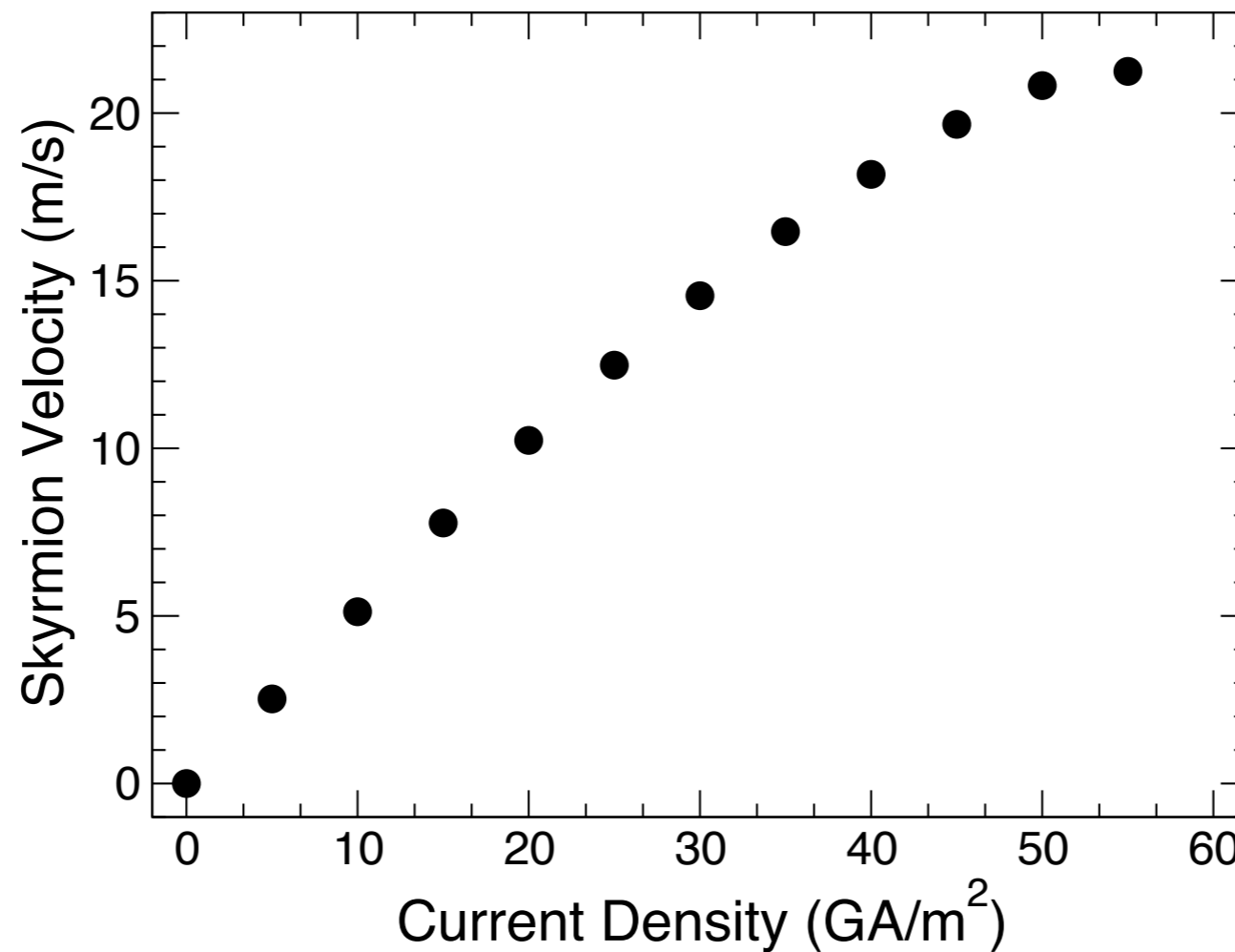
Estimating frequency from edge velocities

F. Garcia-Sanchez *et al.*, New J. Phys. (2016)



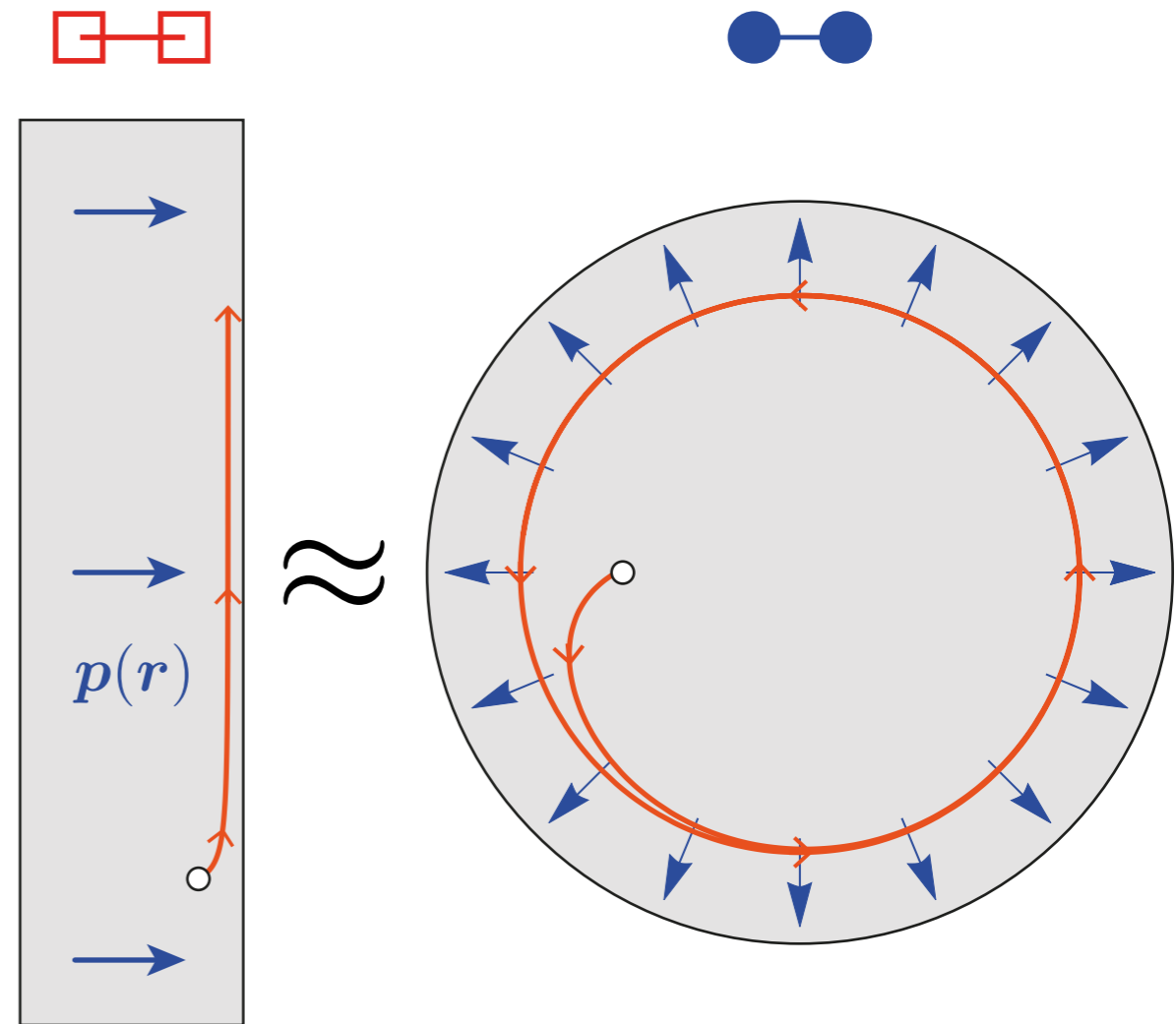
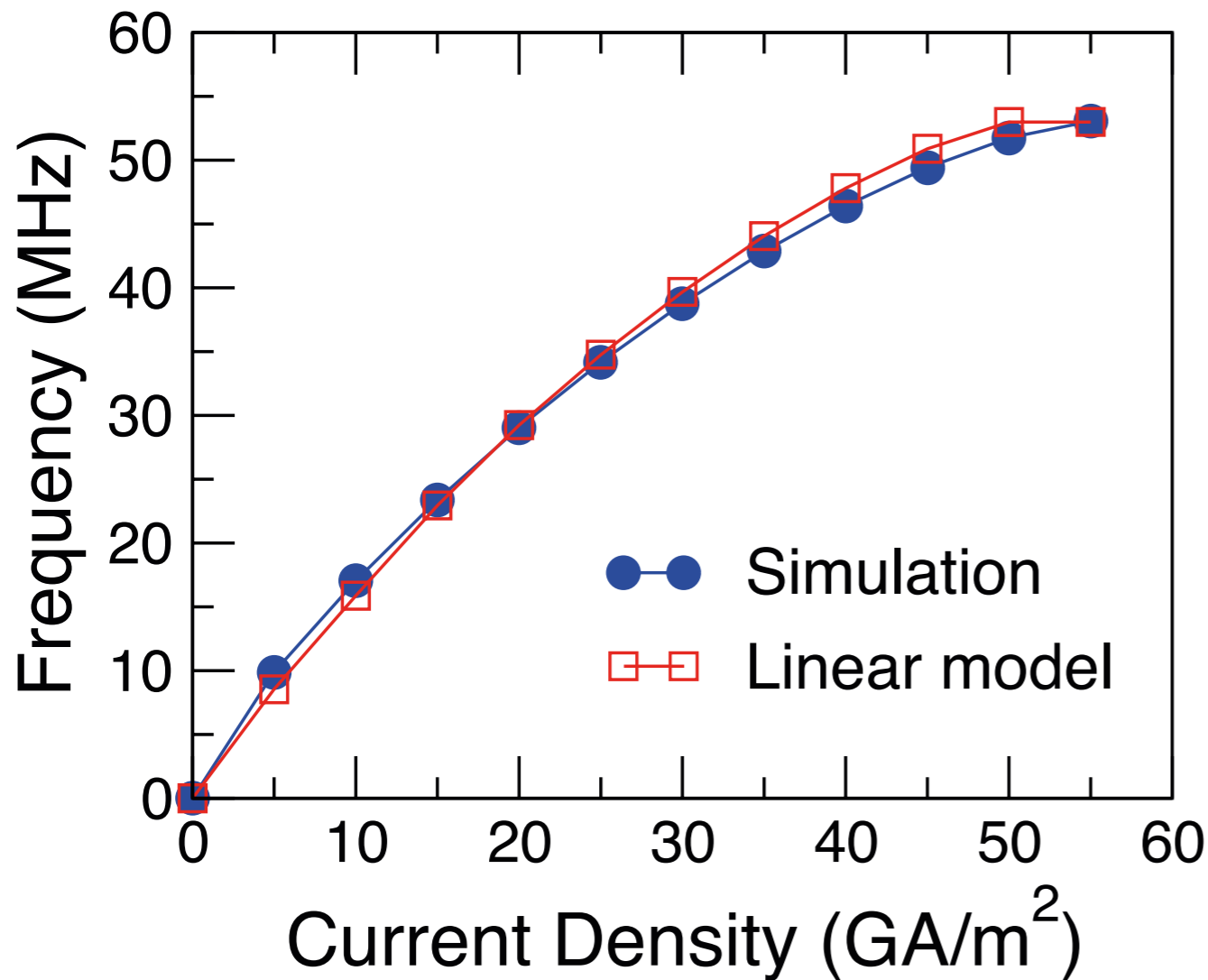
Use the skyrmion velocity along a straight edge (uniform polarizer) to predict oscillation frequency

$J_0 = 50 \text{ GA/m}^2$



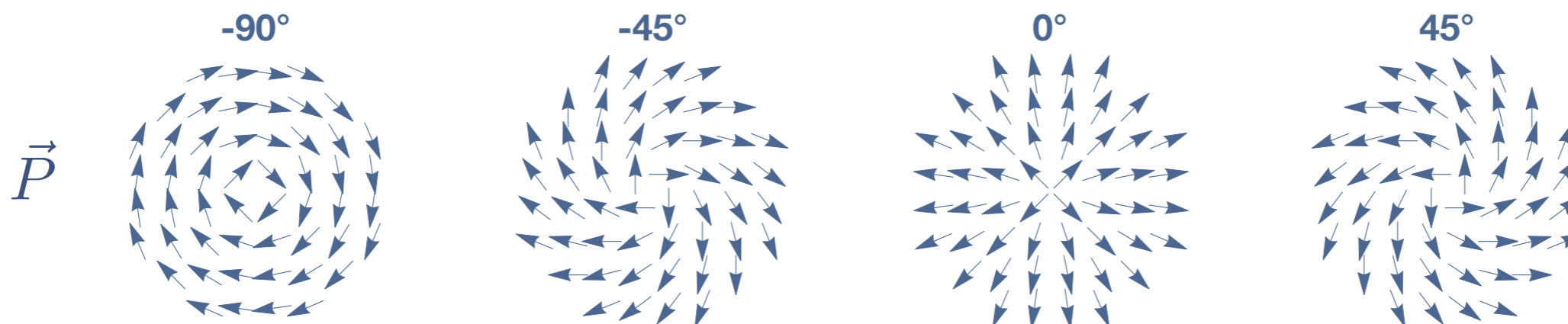
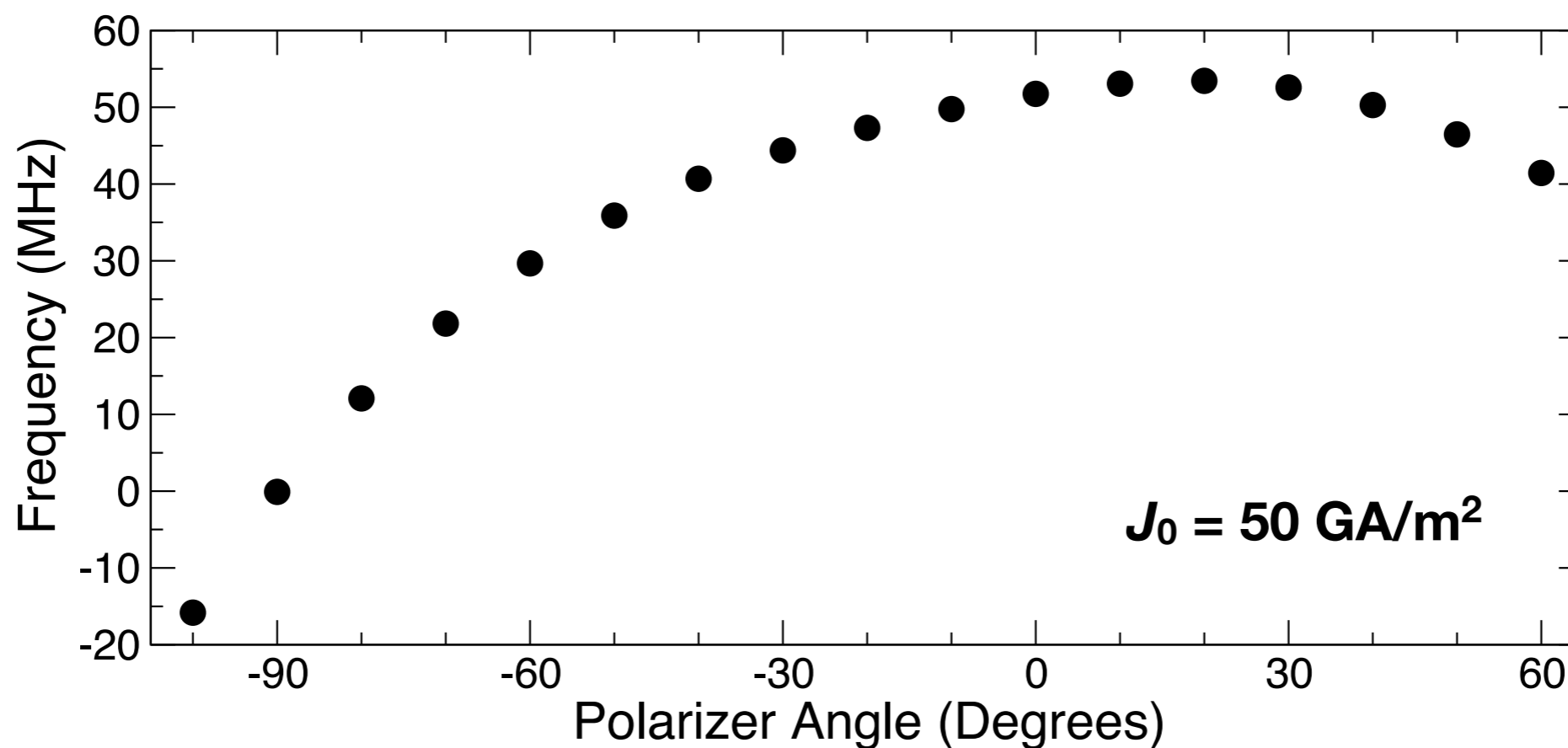
$$f = \frac{1}{2\pi} \frac{v}{r}$$

Estimate frequency from edge velocity and distance from edge





Similar oscillations are observed for different vortex polarizer configurations

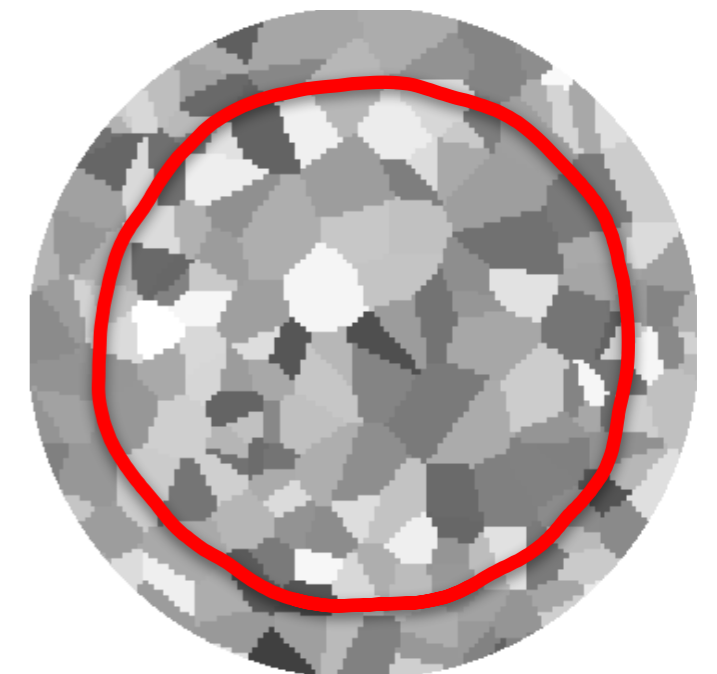
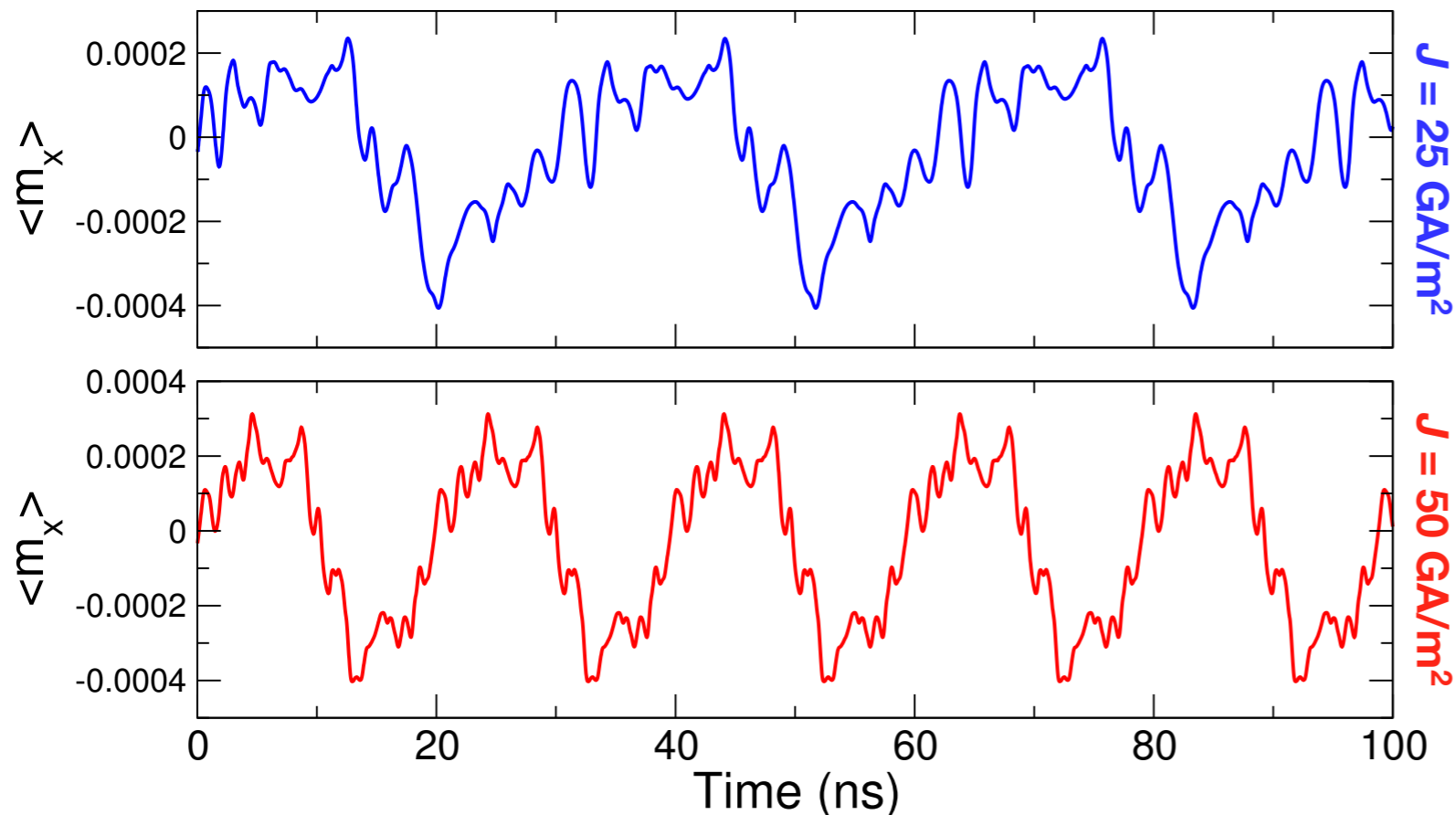
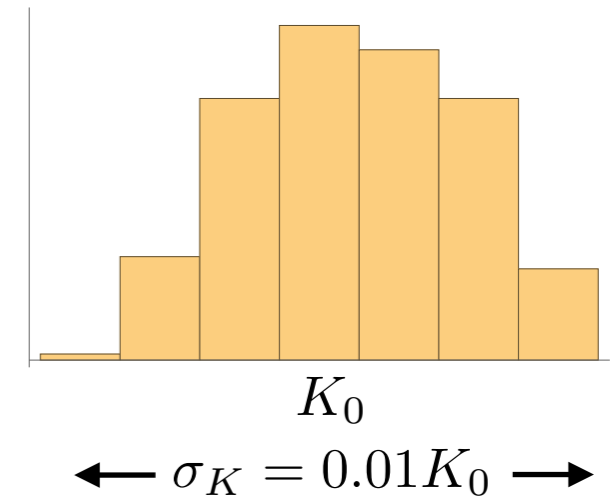


Role of grains and anisotropy distributions

F. Garcia-Sanchez *et al.*, New J. Phys. (2016)

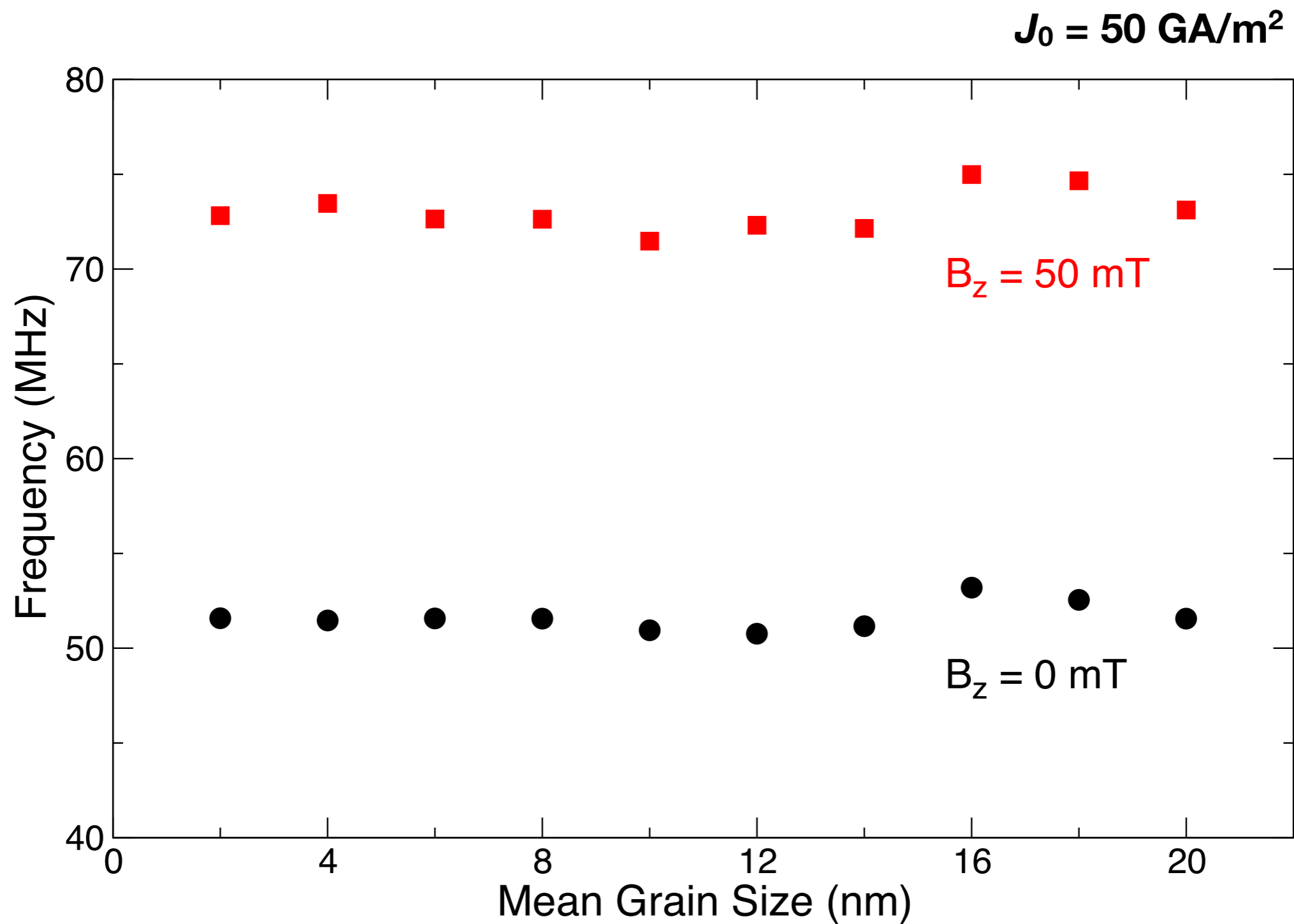


- Modeled defects with distribution of grains with different anisotropies (Gaussian)
- Distorted trajectories with no evidence of athermal spectral line broadening



Mean grain size = 10 nm

- Frequencies largely independent of grain size



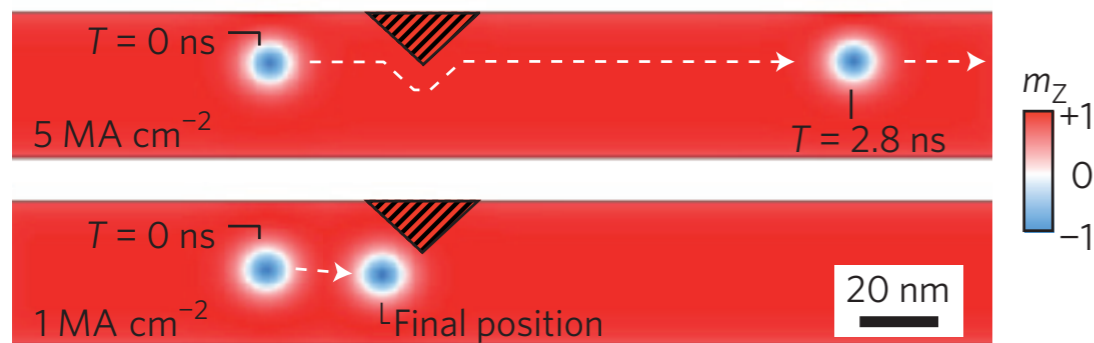


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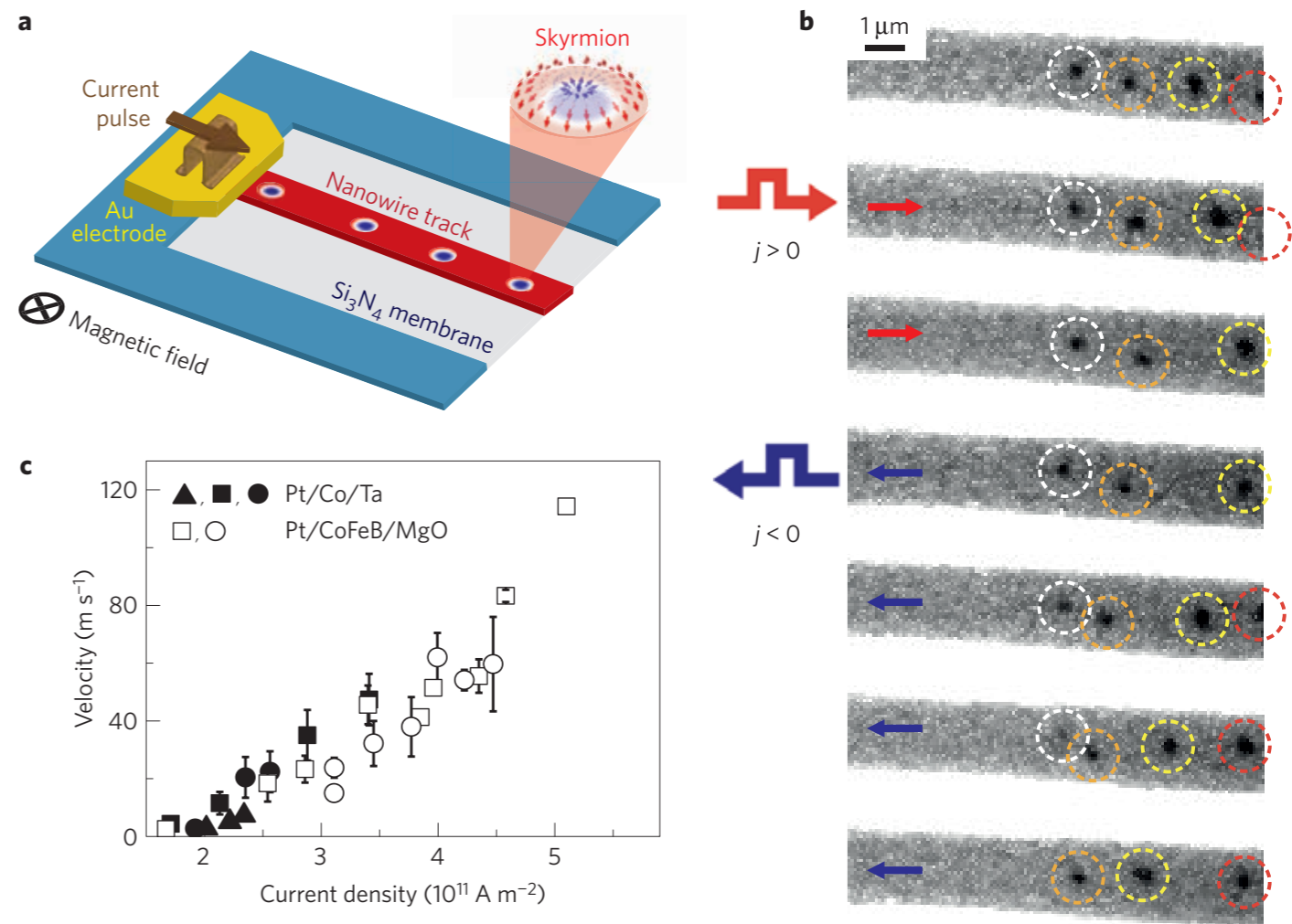
Role of disorder in current-driven skyrmion motion



- **Q:** What is the role of (anisotropy) defects in current-driven skyrmion motion?
- **Q:** Is “topological protection” relevant, or do skyrmions just get pinned like *domain walls*?



J. Sampaio *et al.*, Nat. Nanotech. 2013



S. Woo *et al.*, Nat. Mater. 2016

What can domain wall dynamics teach us?



- In PMA materials, domain wall pinning is an important issue and remains key roadblock for racetrack-type applications
- Pinning leads to finite threshold field or current for propagation

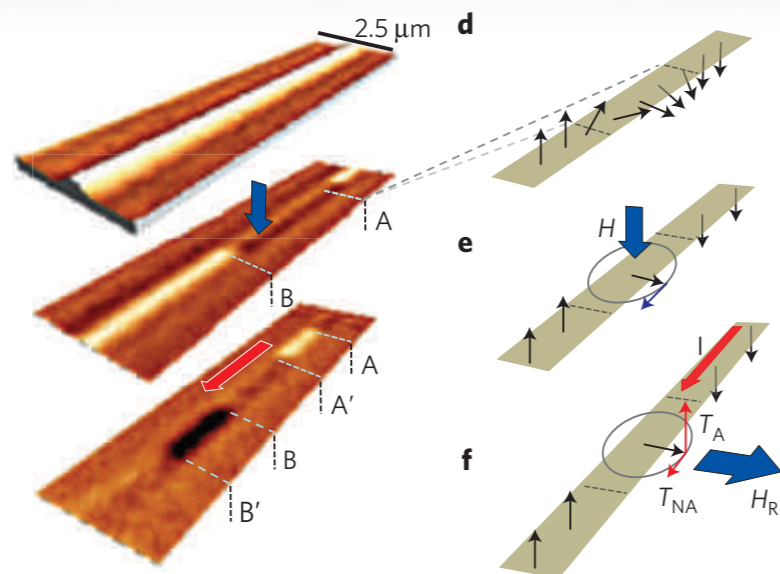
nature
materials

LETTERS

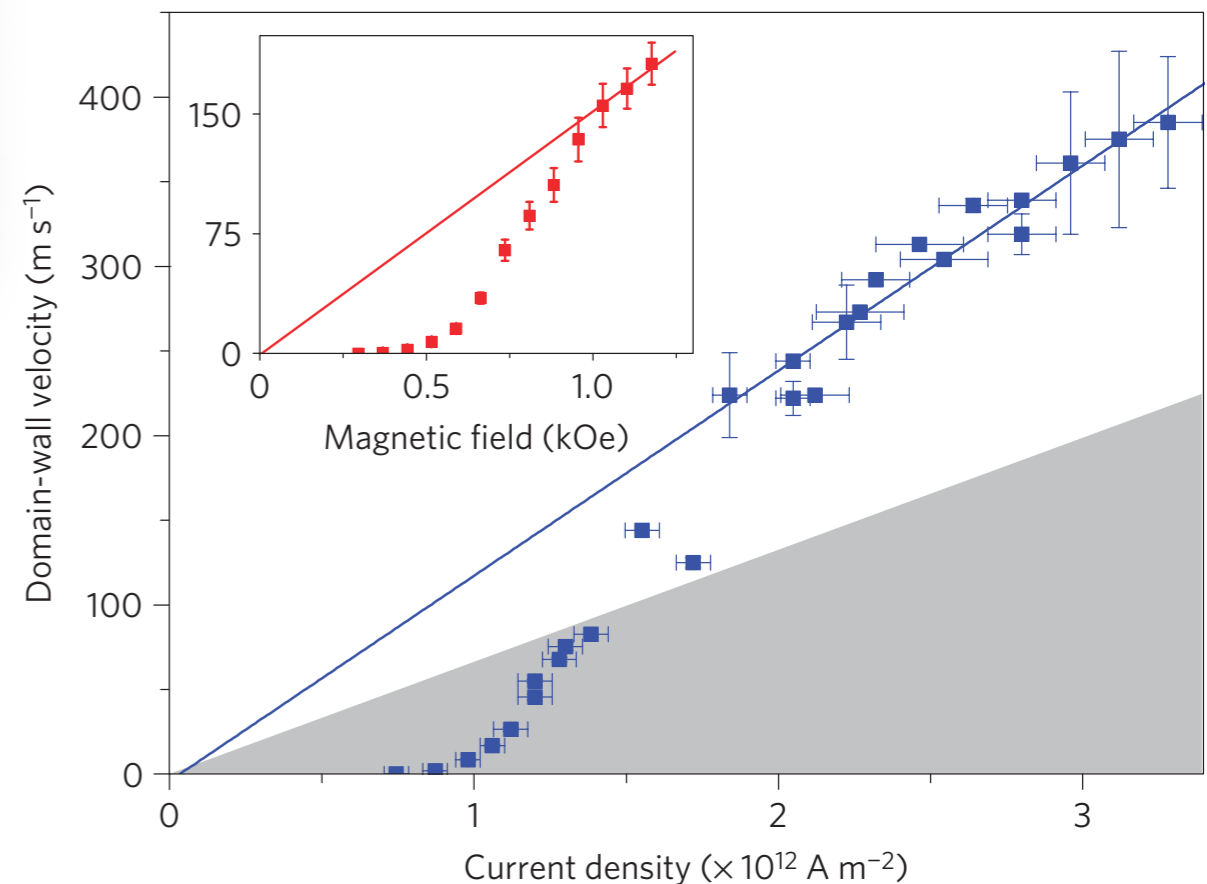
PUBLISHED ONLINE: 15 MAY 2011 | DOI: 10.1038/NMAT3020

Fast current-induced domain-wall motion controlled by the Rashba effect

Ioan Mihai Miron^{1,2*}, Thomas Moore^{1,3}, Helga Szabolics¹, Liliana Daniela Buda-Prejbeanu¹, Stéphane Auffret¹, Bernard Rodmacq¹, Stefania Pizzini³, Jan Vogel³, Marlio Bonfim⁴, Alain Schuhl^{1,3} and Gilles Gaudin¹



Pt/Co (0.6 nm)/AlO_x
Néel wall (DMI) + spin Hall effect



- For field-driven dynamics, motion at low fields occurs in *creep regime*

Universal Pinning Energy Barrier for Driven Domain Walls in Thin Ferromagnetic Films

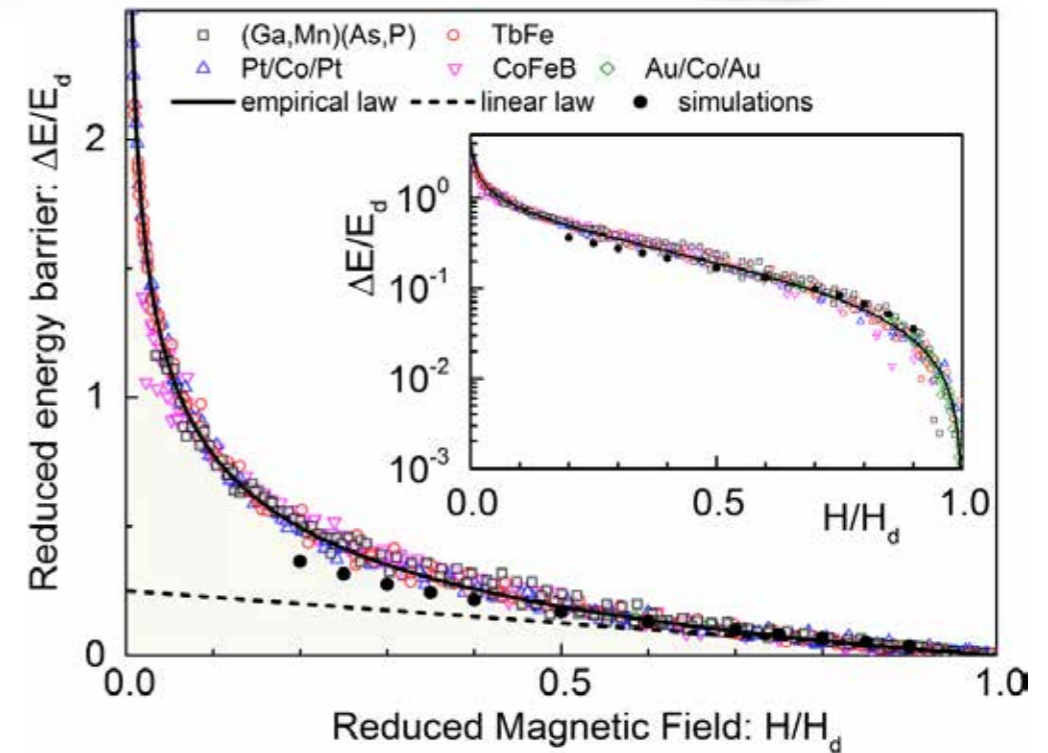
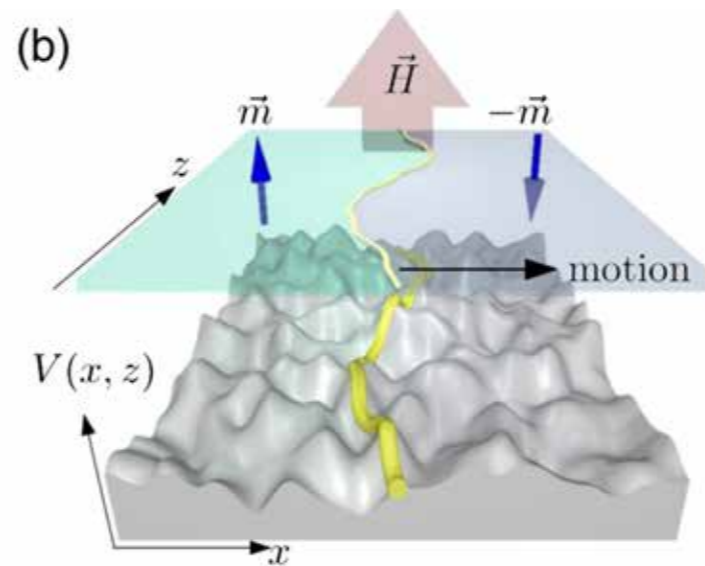
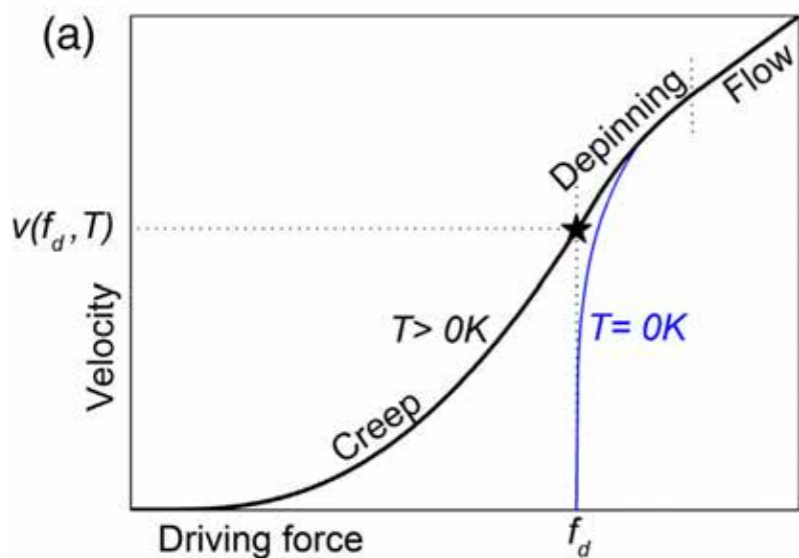
V. Jeudy,^{1,†} A. Mougin,¹ S. Bustingorry,² W. Savero Torres,¹ J. Gorchon,¹ A. B. Kolton,² A. Lemaître,³ and J.-P. Jamet^{1,*}

¹Laboratoire de Physique des Solides, CNRS, Univ. Paris-Sud, Université Paris-Saclay, 91405 Orsay Cedex, France

²CONICET, Centro Atómico Bariloche, 8400 San Carlos de Bariloche, Río Negro, Argentina

³Laboratoire de Photonique et de Nanostructures, CNRS, Université Paris-Saclay, 91460 Marcoussis, France

(Received 8 March 2016; published 29 July 2016)



$$v = v_0 \exp \left(-\beta_d \left[\left(\frac{H}{H_d} \right)^{-1/4} - 1 \right] \right)$$

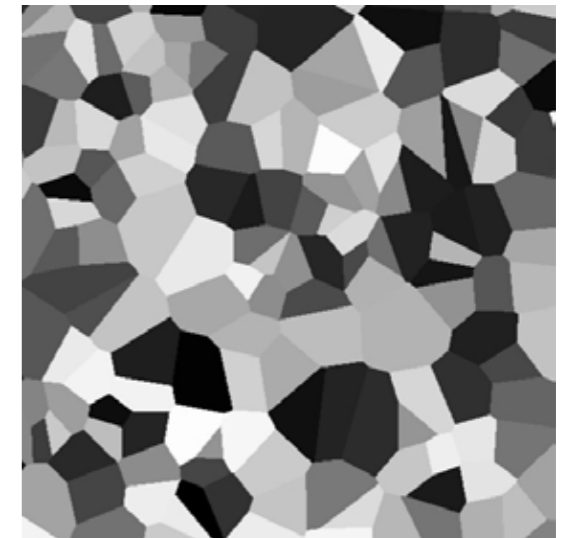
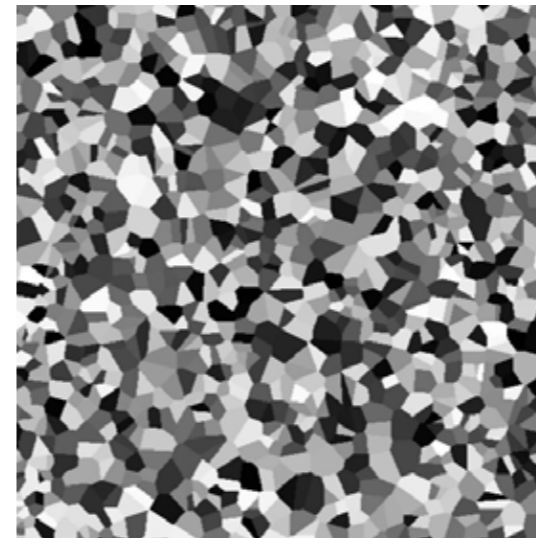
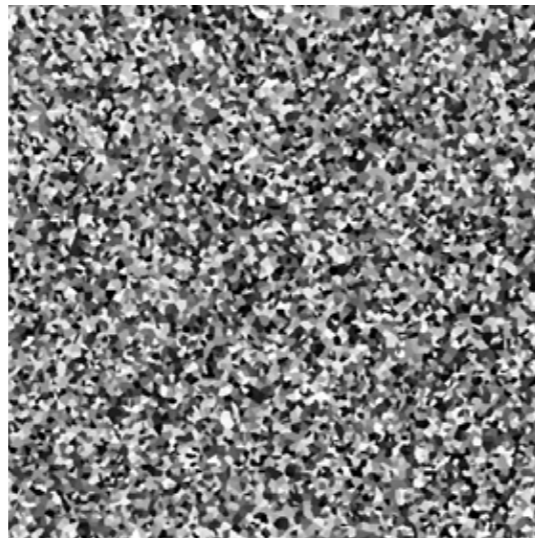
- Proposal: Depinning field, H_d , is a useful material parameter for characterizing disorder (even for skyrmion dynamics)

$$v = v_0 \exp \left(-\beta_d \left[\left(\frac{H}{H_d} \right)^{-1/4} - 1 \right] \right)$$

| Material | Thick. (nm) | $T(K)$ | $T_d(K)$ | $H_d(mT)$ | $v(H_d)(m/s)$ |
|---------------|----------------|--------|------------|-----------|---------------|
| (Ga,Mn)(As,P) | 12 | 10 | 616(10) | 6.2(0.1) | 1.8(0.1) |
| | | 30 | 1440(20) | 5.8(0.1) | 1.8(0.1) |
| | | 50 | 1140(20) | 5.6(0.1) | 2.0(0.2) |
| | | 65 | 815(10) | 5.5(0.1) | 2.3(0.1) |
| TbFe | 5×1.8 | 271 | 5750(50) | 295(5) | 1.4(0.1) |
| | | 289 | 4200(50) | 225(5) | 1.8(0.1) |
| | | 304 | 3050(50) | 130(5) | 1.7(0.1) |
| | | 310 | 2600(50) | 100(5) | 1.7(0.1) |
| | | 315 | 2200(50) | 80(5) | 1.8(0.1) |
| Pt/Co/Pt | 0.5 | 293 | 2558(10) | 28.5(2) | 5.7(0.2) |
| | | | 4145(25) | 56(1) | 10.6(1.0) |
| | | | 6490(30) | 76(1) | 16.6(1.0) |
| | | | 9720(45) | 72(1) | 18.4(1.0) |
| | | | irradiated | 0.5 | 2260(50) |

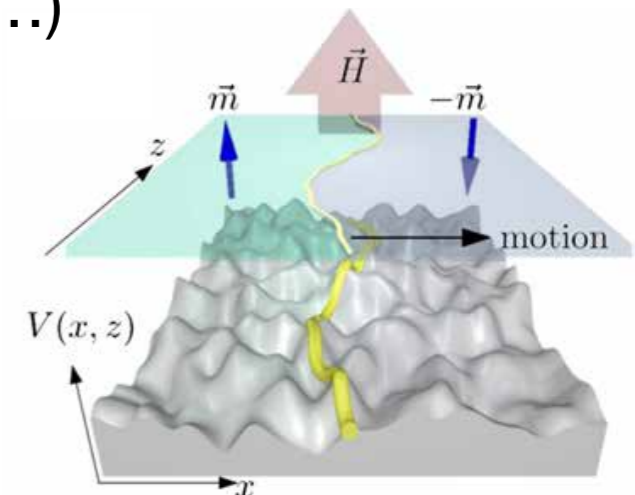
V. Jeudy *et al.*, Phys. Rev. Lett. 2016 (Supplementary)

Simulating disorder with micromagnetics

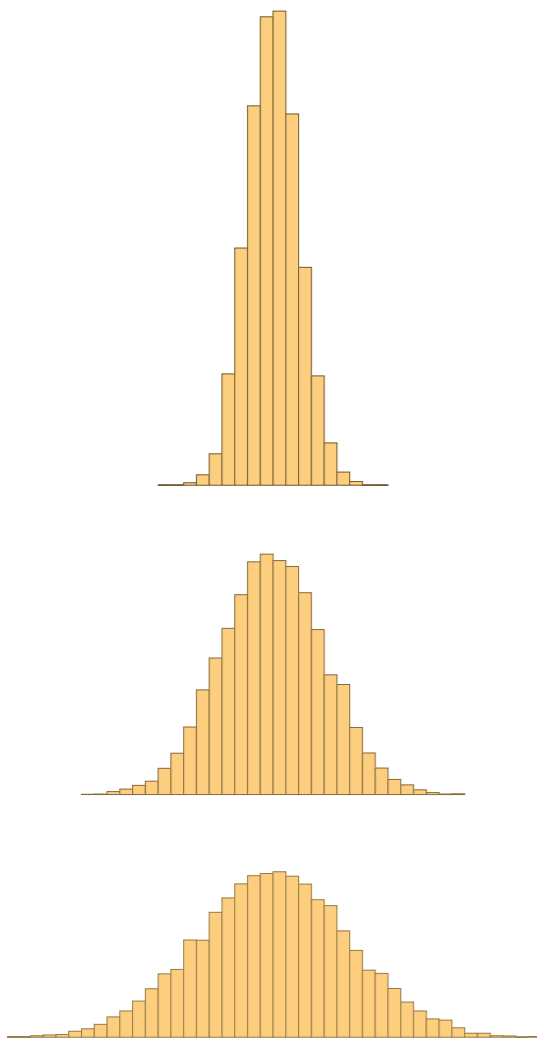


→ vary average grain size

- Simulate disorder using random grain distribution with different anisotropies
- Anisotropy variation leads to random potential for domain walls (and skyrmions ...)



↓ vary spread in (Gaussian) distribution of K_u

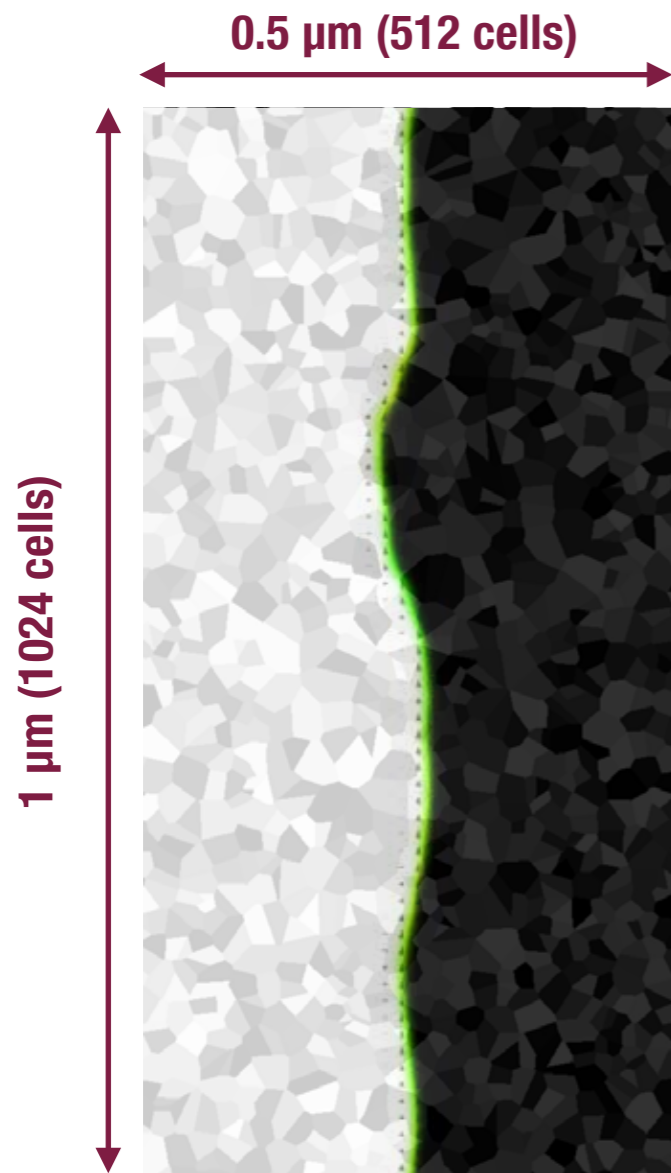


Simulating domain wall depinning

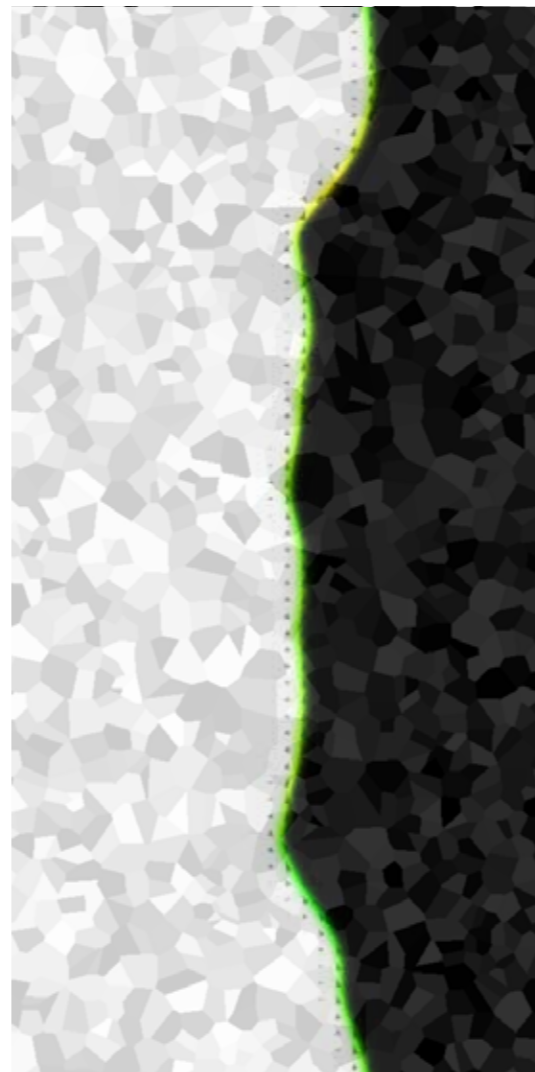


- Minimize energy at each field step

avg. grain size = 20 nm
10% variation in K_u



$H = 0$



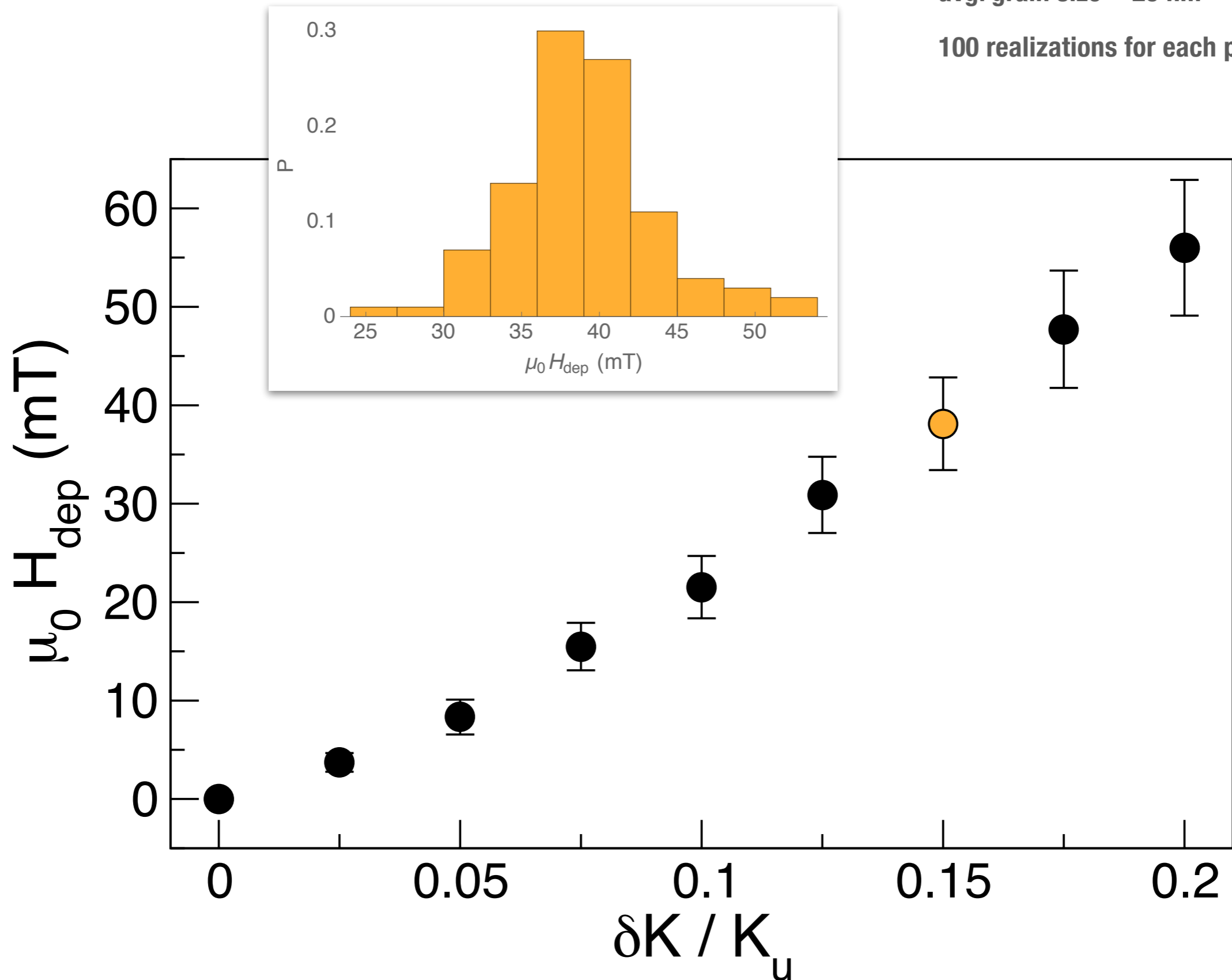
$H < H_{\text{dep}}$



$H > H_{\text{dep}}$

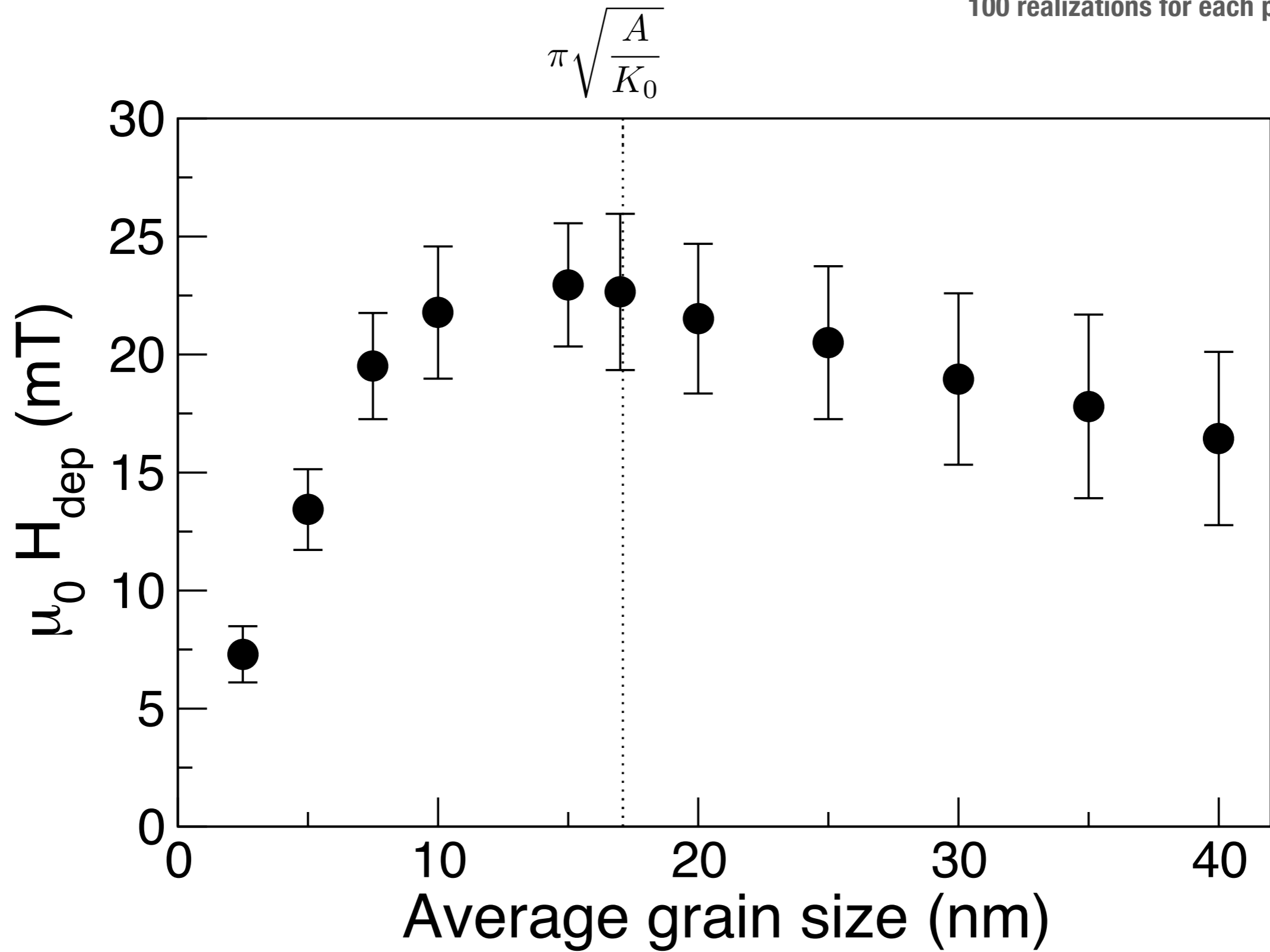
avg. grain size = 20 nm

100 realizations for each point



10% anisotropy variation

100 realizations for each point

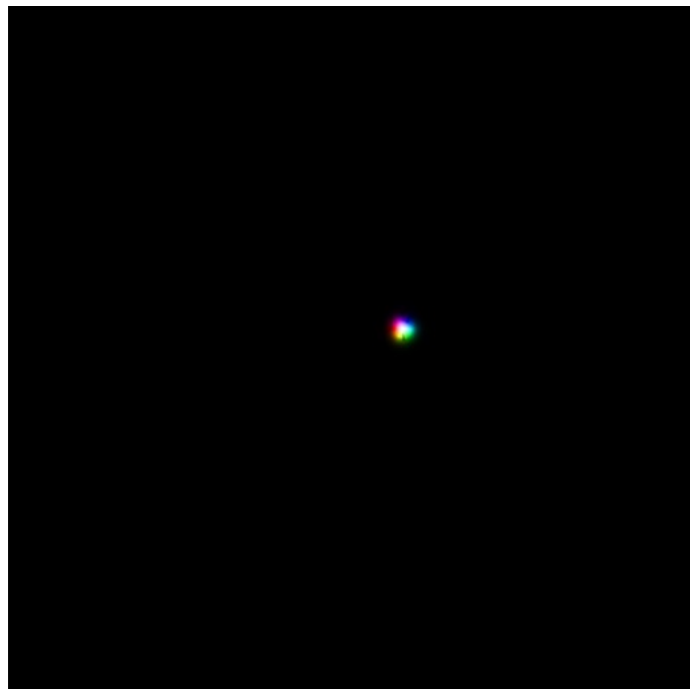


Simulating current-driven skyrmion motion ($T = 0$ K)

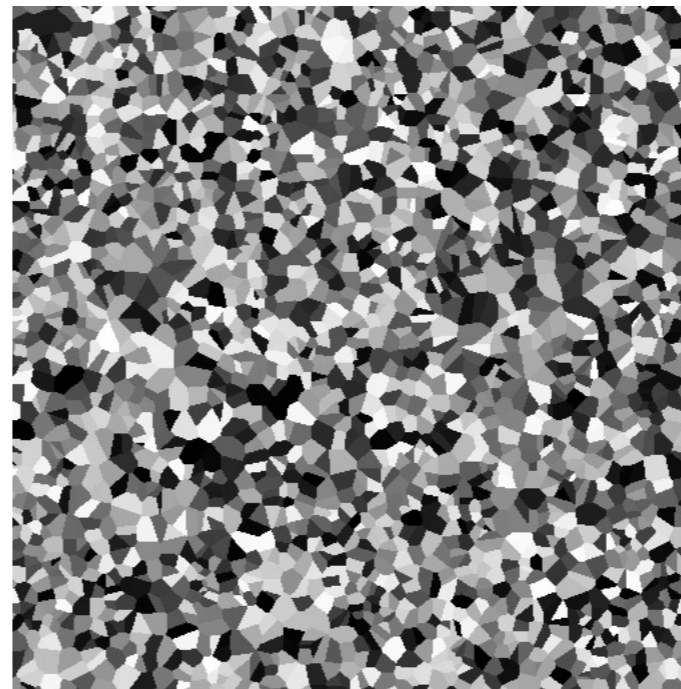
J.-V. Kim *et al.*, arXiv:1701.08357



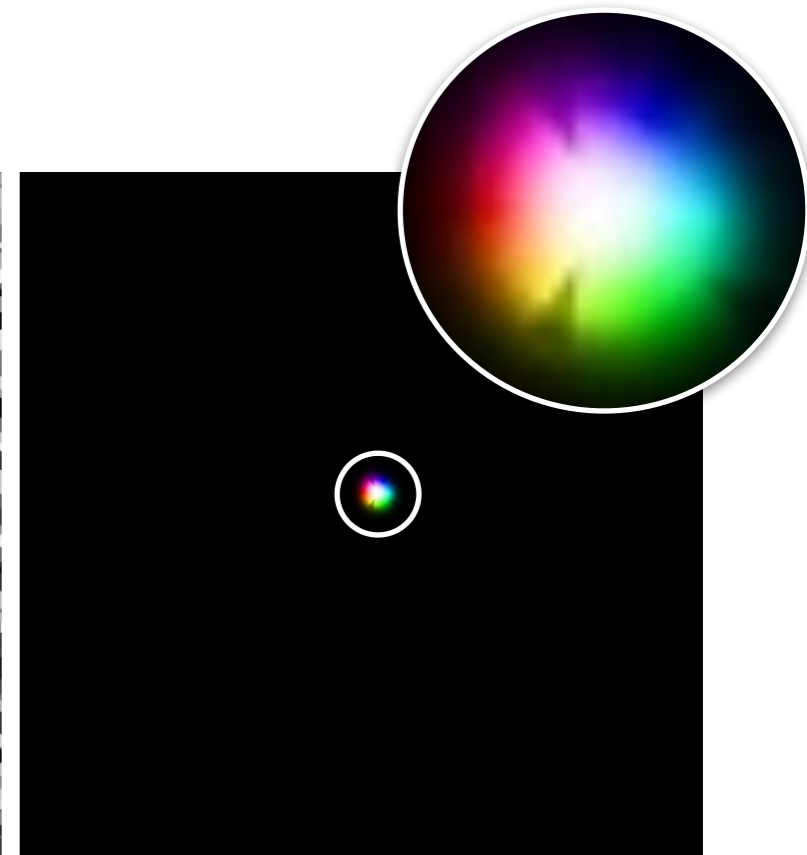
0.5 μm (512 cells), PBC



clean system



disordered system

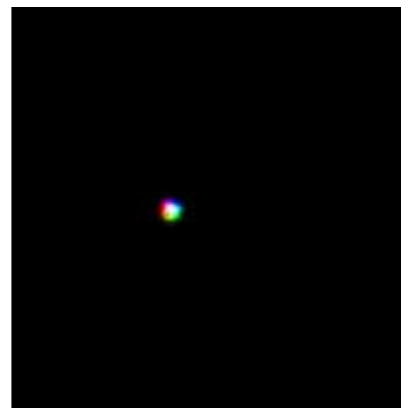


- For each current density, considered 50 different realizations of disorder
- For each realization, applied current during 10 ns (*)
- Velocity for each current density averaged over the 50 realizations

Possible scenarios

1. Propagation

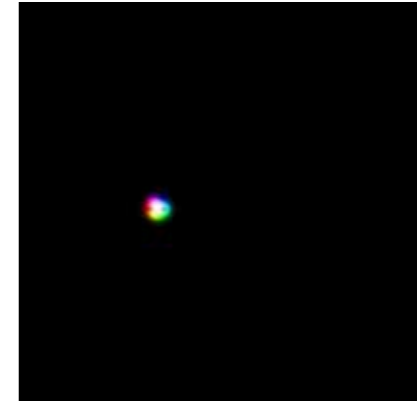
$t = 0$



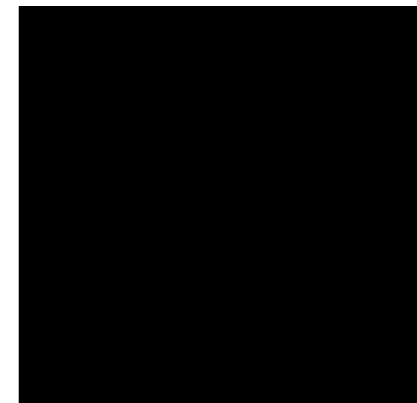
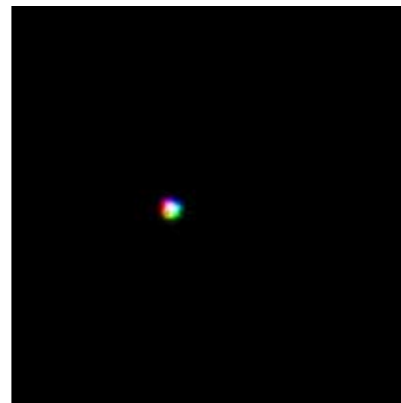
$t = t_{\text{final}}$



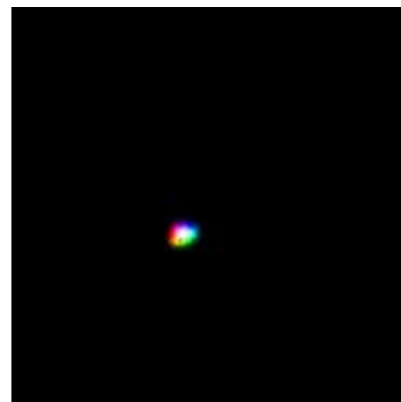
2. Pinned



3. Annihilation

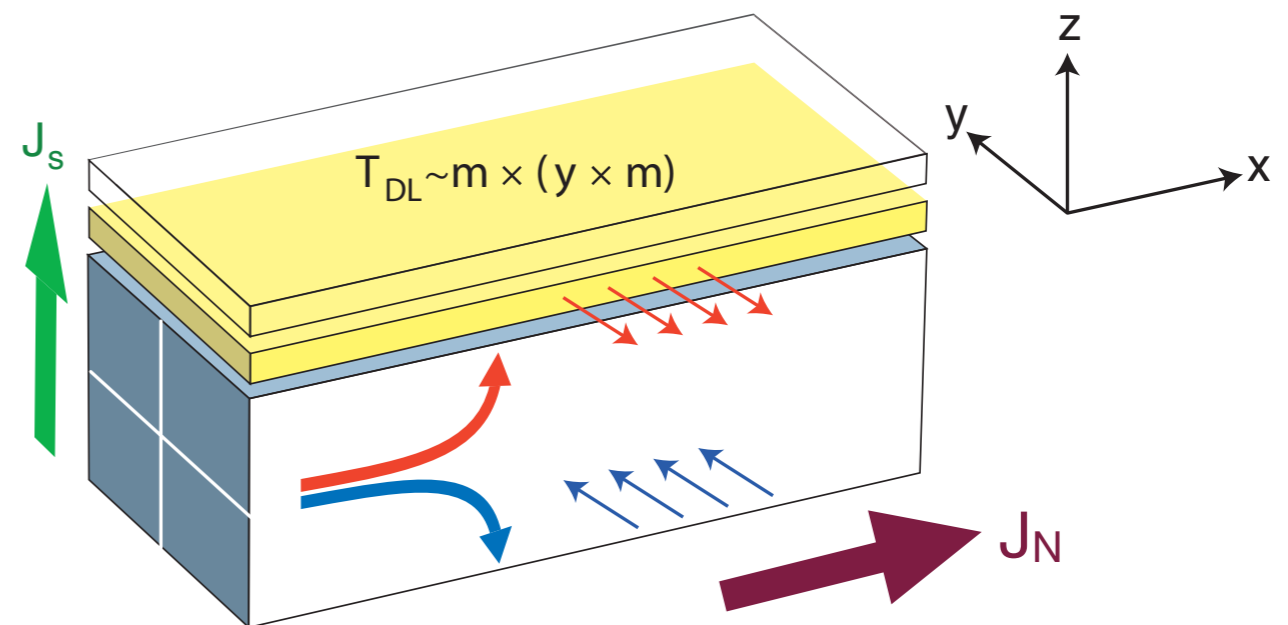


4. Explosion (SHE)

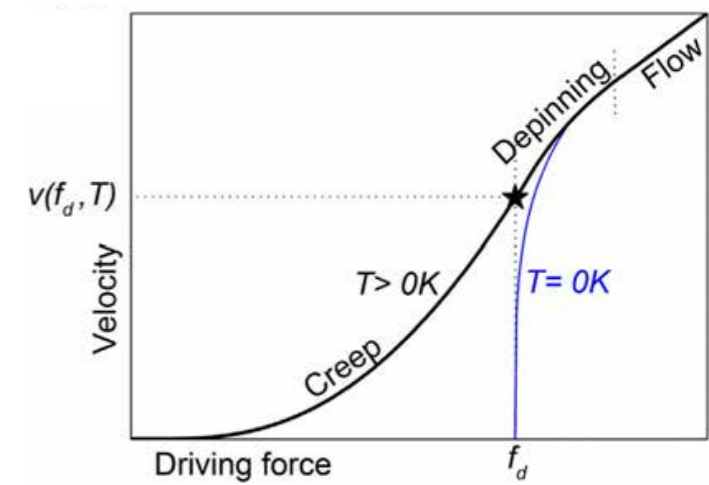
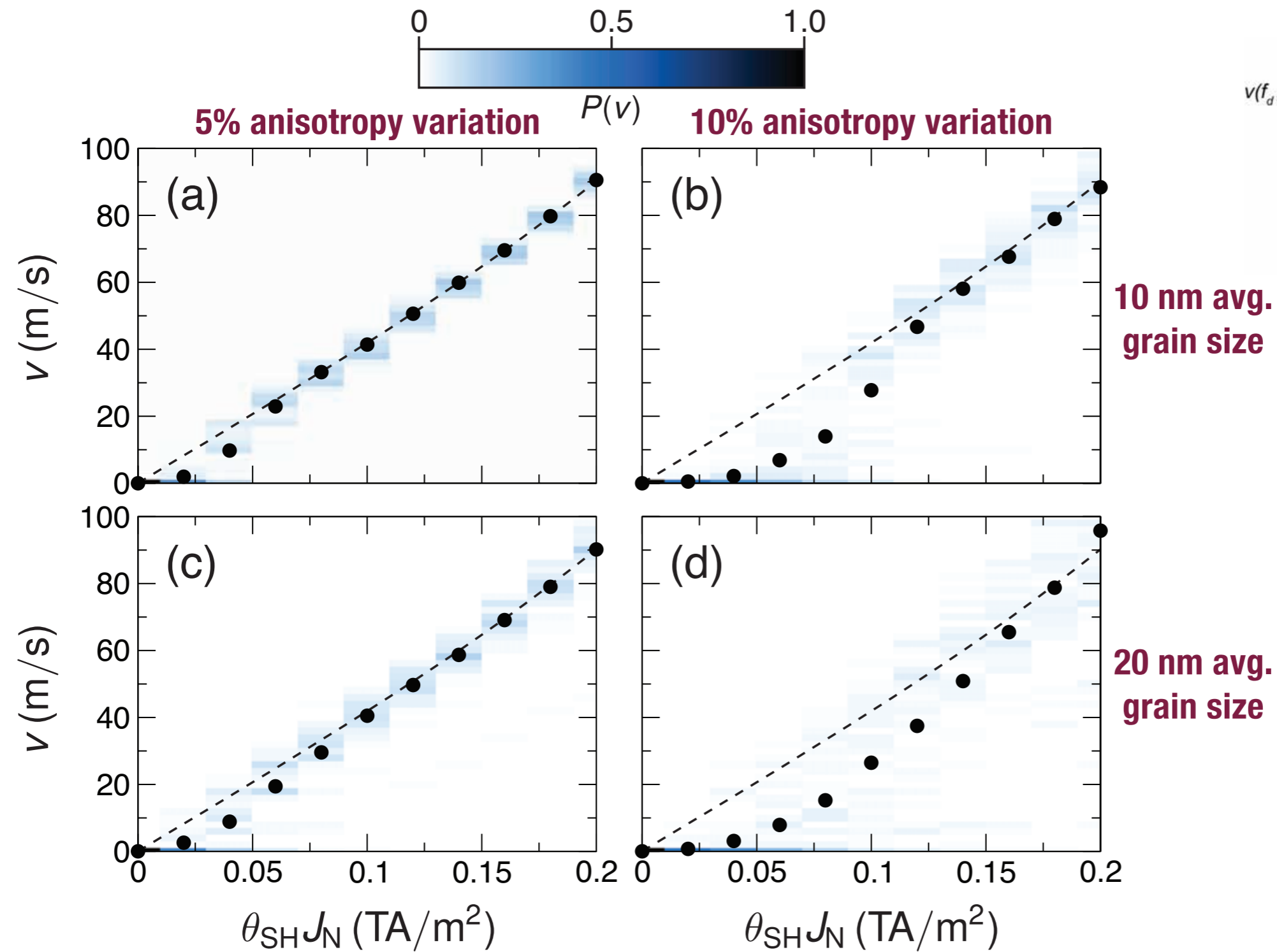




- Considered spin torques due to the spin Hall effect
- Implicit assumption: Current density J_N flows through a heavy-metal under layer along x (e.g., Pt, W, ...), which leads to spin current polarized along y that flows in the z direction.
- Caveat: currents must be below switching current at which magnetization is aligned // y .



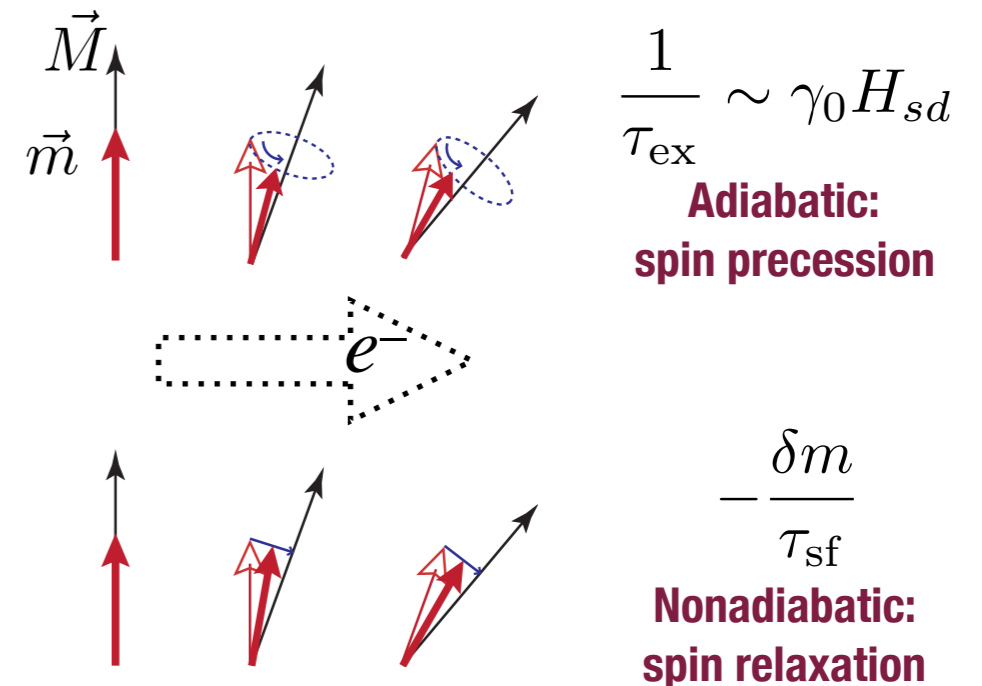
$$\frac{d\mathbf{m}}{dt} = -|\gamma|\mu_0\mathbf{m} \times \mathbf{H}_{\text{eff}} + \alpha\mathbf{m} \times \frac{d\mathbf{m}}{dt} + \frac{\hbar\gamma}{2eM_s d}\theta_{\text{SH}}J_N\mathbf{m} \times (\mathbf{m} \times \hat{y})$$



- Pinning observed at low currents, disorder-free regime attained as current is increased.



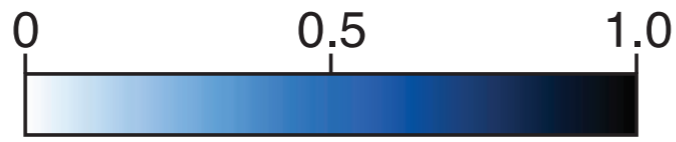
- Also considered spin torques due to current flow through ferromagnet
- Implicit assumption: Uniform current density J_F leads to torques that depend on magnetization gradients (Zhang-Li model)
- Caveat: currents must be below instability threshold for uniform magnetization state



$$\mathbf{u} = (\hbar\gamma/2eM_s)P \mathbf{J}_F$$

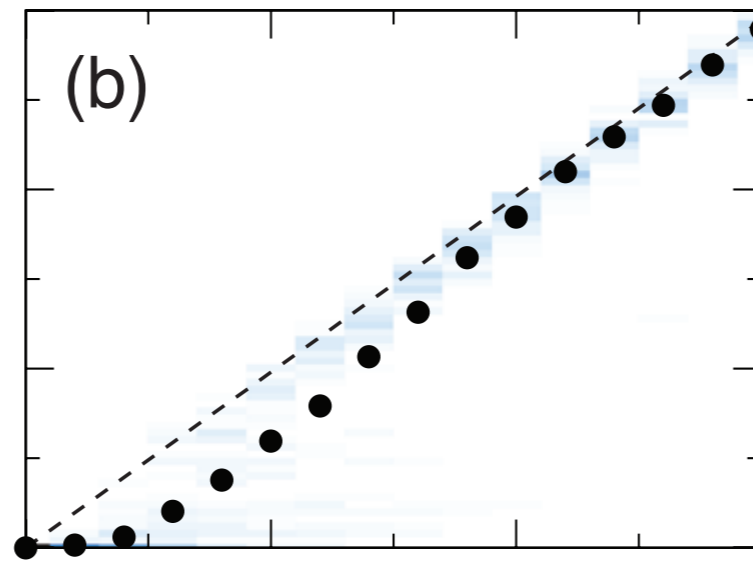
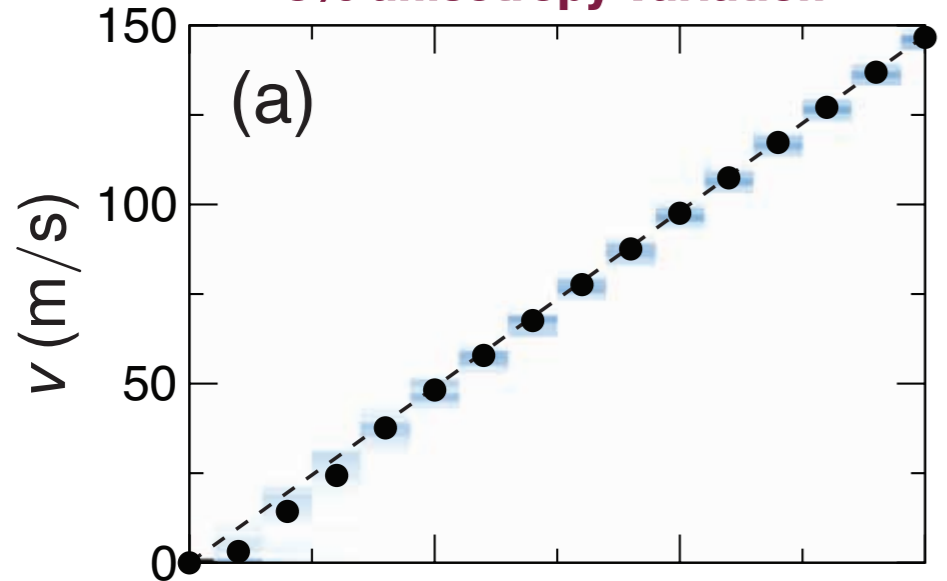
Effective spin current drift velocity

$$\frac{d\mathbf{m}}{dt} = -|\gamma|\mu_0 \mathbf{m} \times \mathbf{H}_{\text{eff}} + \alpha \mathbf{m} \times \frac{d\mathbf{m}}{dt} - \underbrace{\mathbf{u} \cdot \nabla \mathbf{m}}_{\text{adiabatic}} + \beta \mathbf{m} \times (\mathbf{u} \cdot \nabla \mathbf{m})_{\text{nonadiabatic}}$$

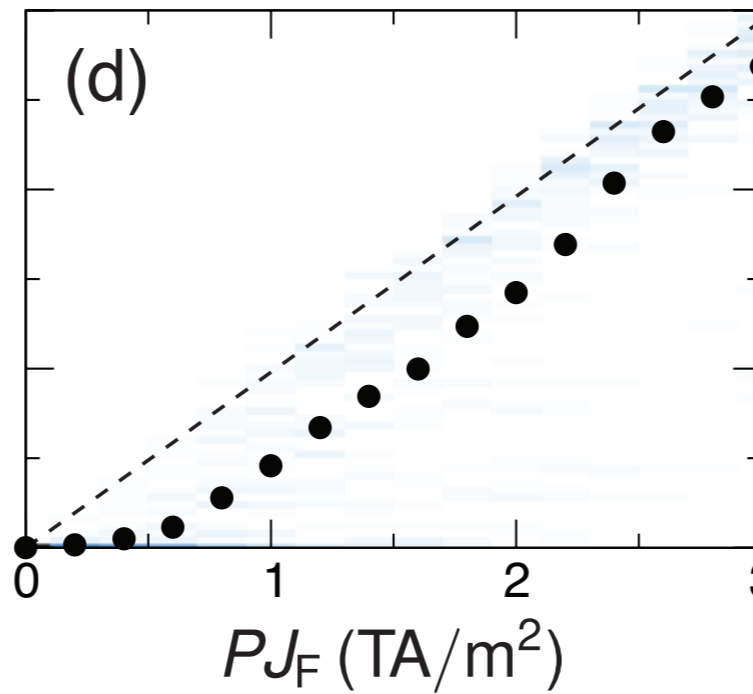
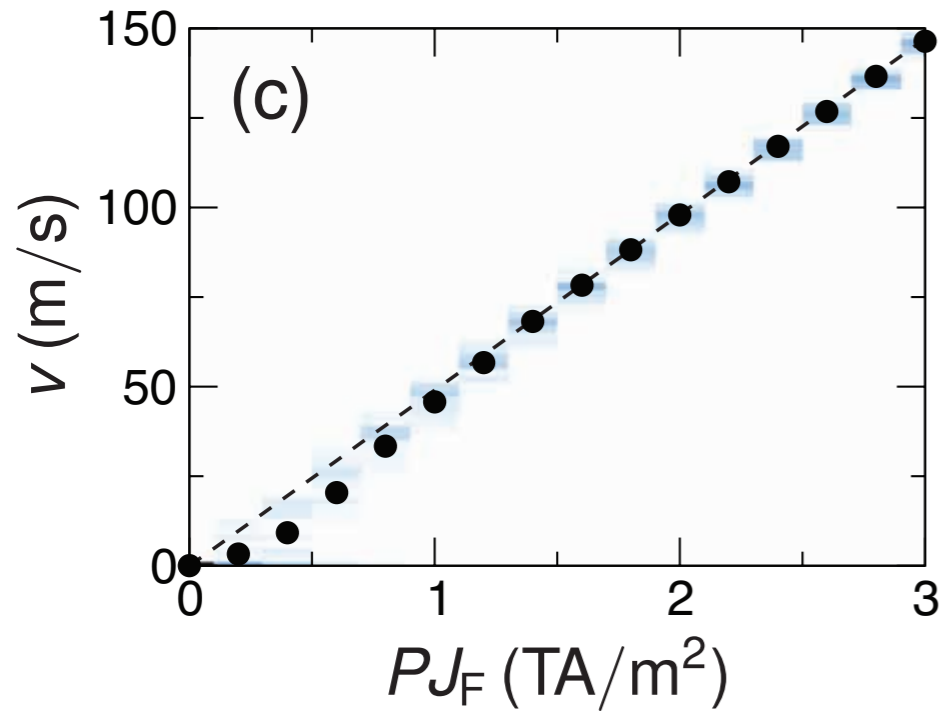


5% anisotropy variation

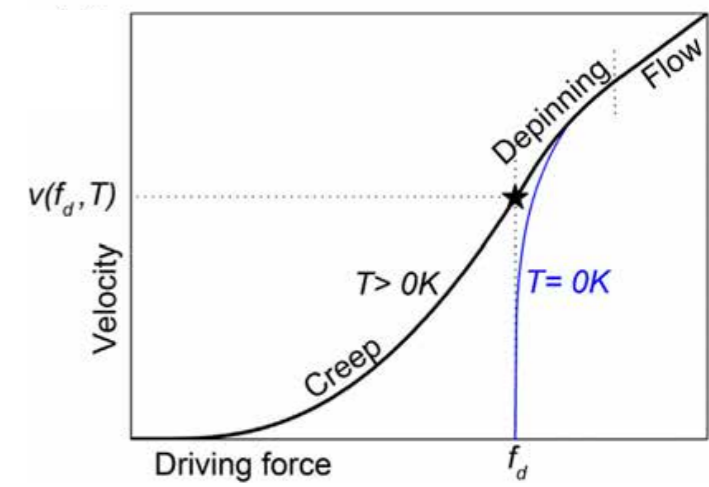
10% anisotropy variation



10 nm avg.
grain size



20 nm avg.
grain size



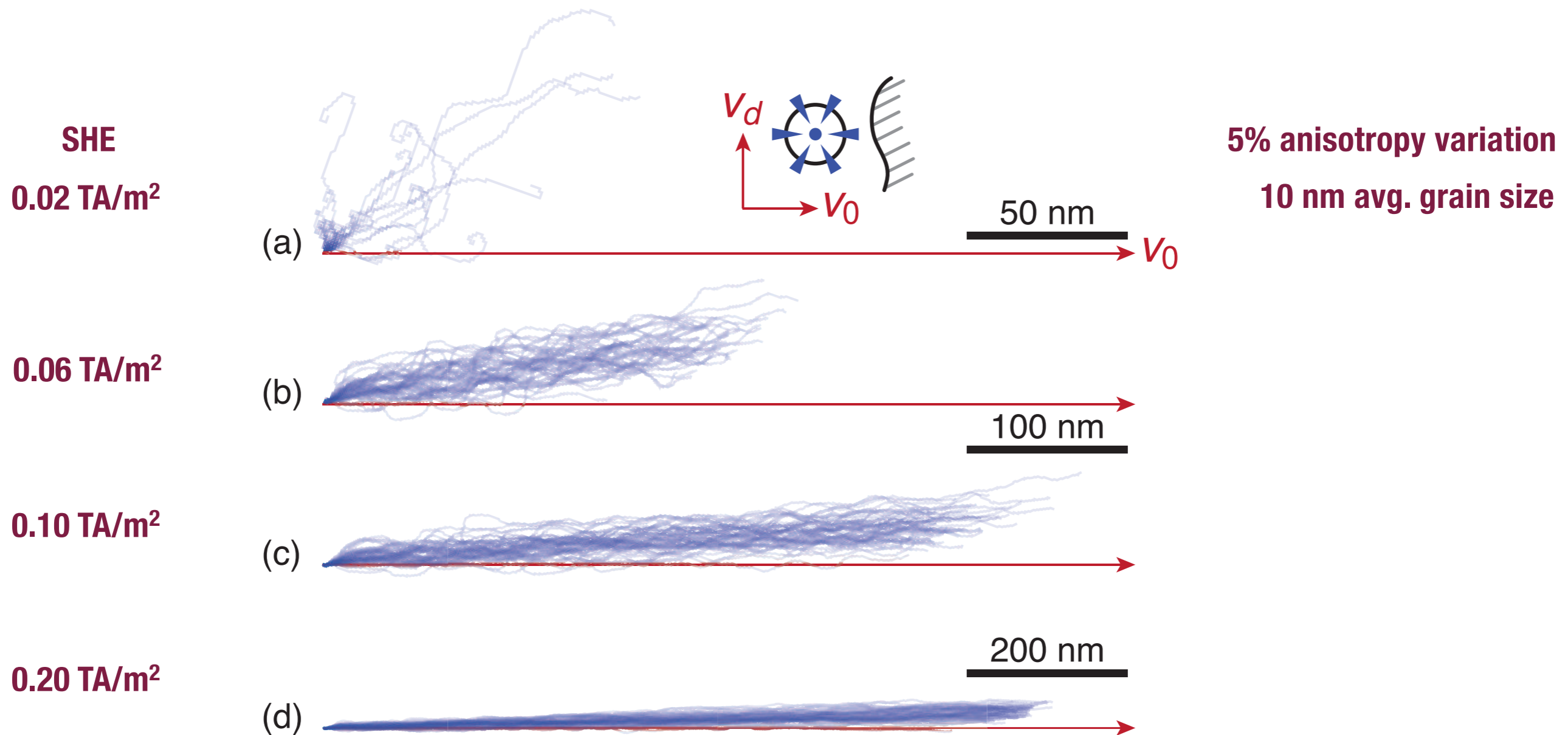
- Similar pinning behavior observed as for SHE-driven motion

Extrinsic skyrmion Hall effect

J.-V. Kim *et al.*, arXiv:1701.08357

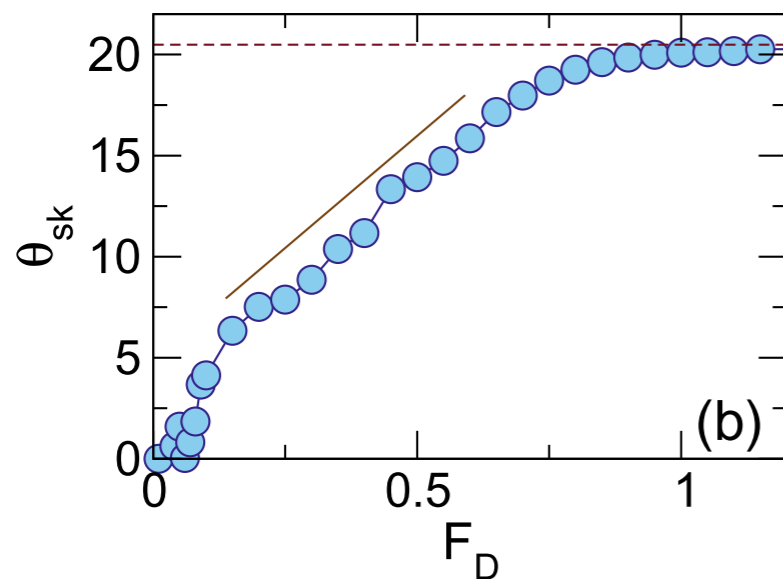
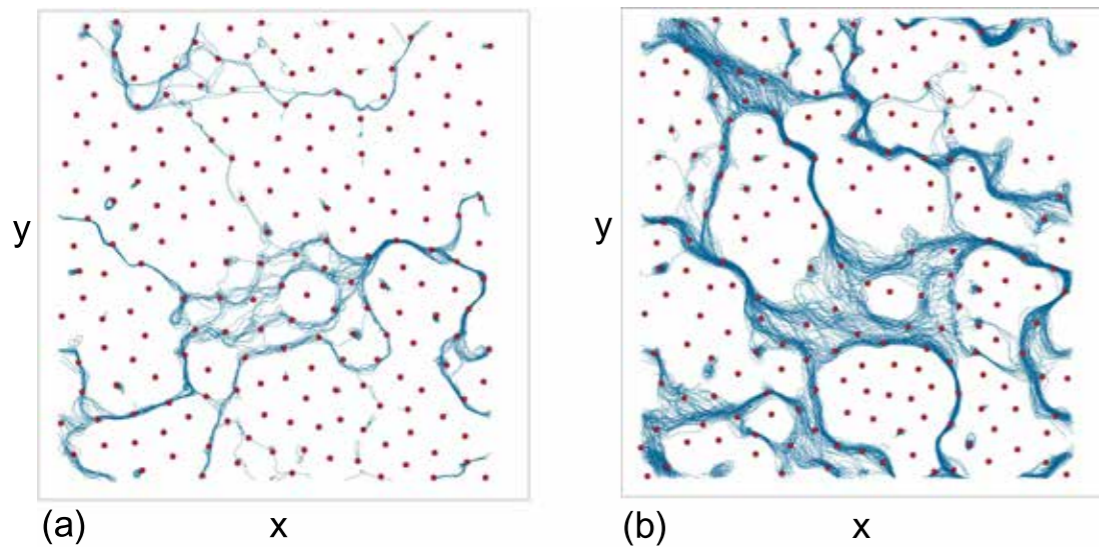


- Disorder-induced local fields lead to jagged motion of skyrmion
- Pinning forces (cf. boundary edges) give rise to additional Hall effect



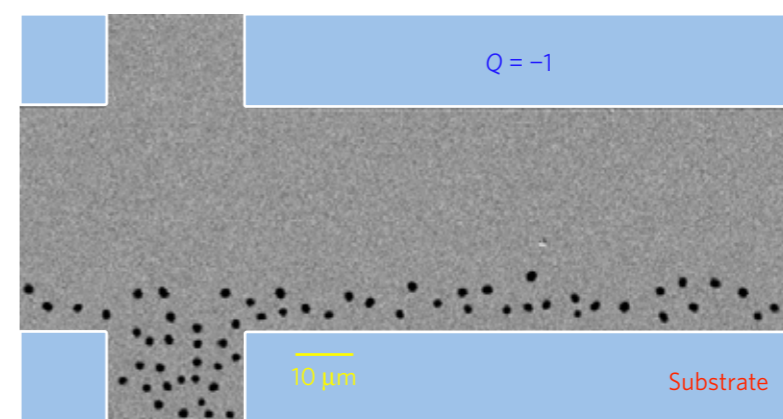
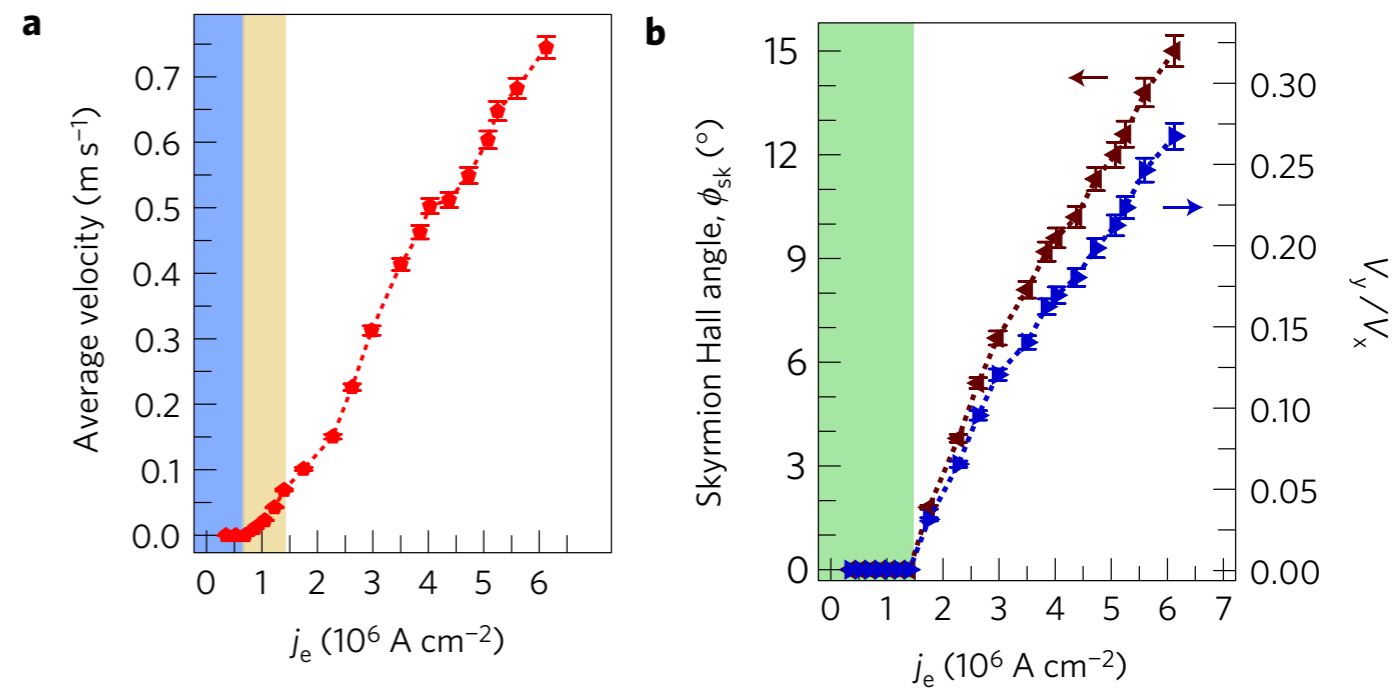
- Behavior consistent with molecular dynamics simulations (hard cores) and recent experimental results

Molecular dynamics



C. Reichhardt *et al.*, New J. Phys. 2016

Experiments on Ta/CoFeB/TaOx



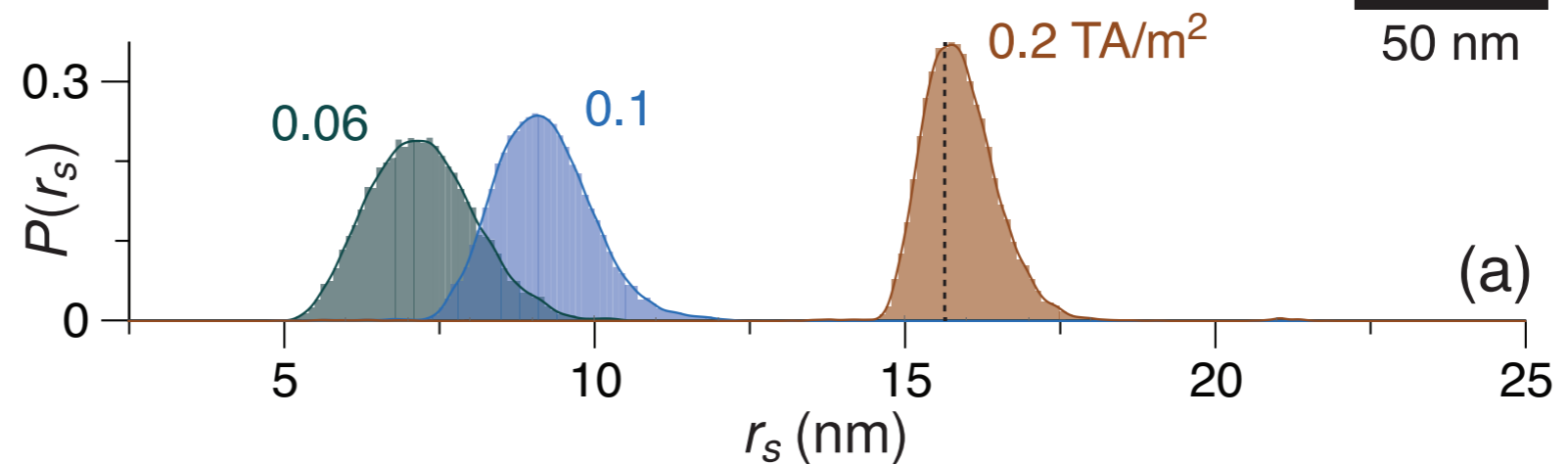
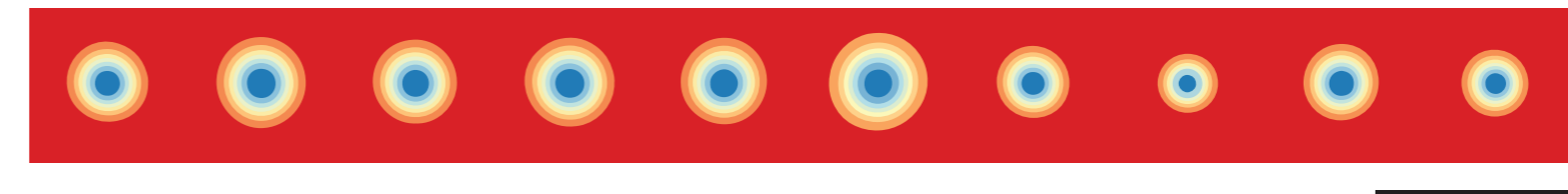
W. Jiang *et al.*, Nat. Phys. 2017

Fluctuations of core size

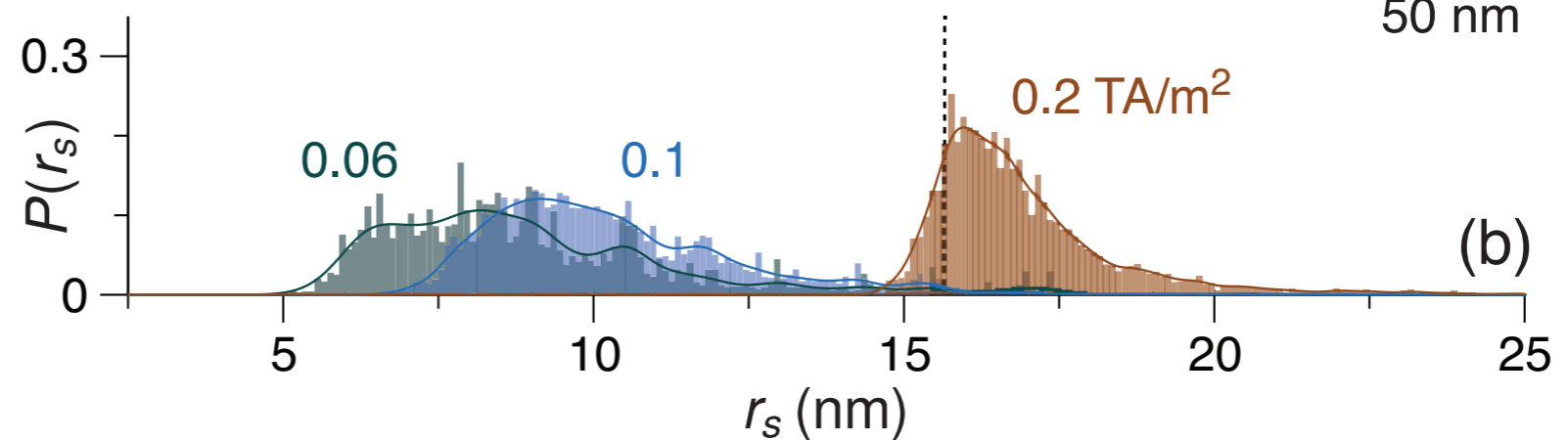
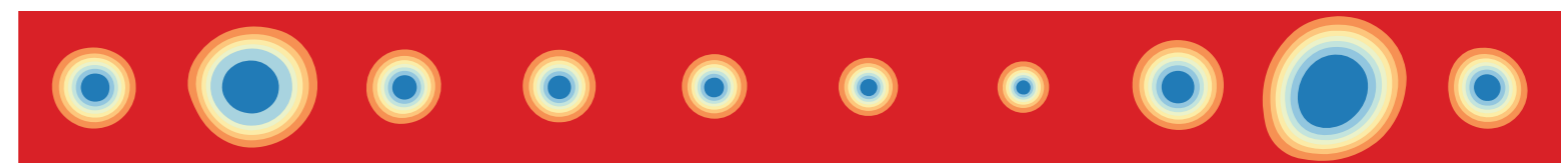


Large variations in core size seen as skyrmion propagates through disordered film

20 nm avg. grain size

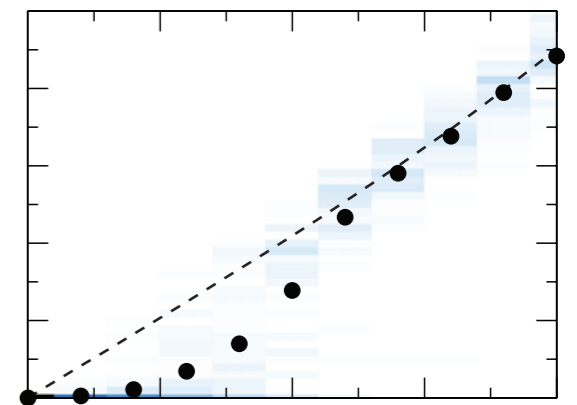
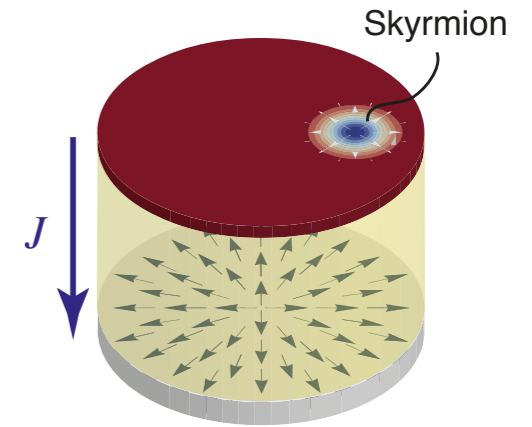


5%
anisotropy
variation



10%
anisotropy
variation

- Examined boundary edge and disorder-induced confinement effects in ultrathin ferromagnets with perpendicular anisotropy:
 - *Skyrmion oscillators with inhomogeneous polarizers* [1]
 - *Current-induced motion in disordered films* [2]
- Disorder can result in strong pinning, finite threshold currents, stochastic motion in realistic films
 - *Undesired effects for information storage applications, possibly no advantages compared with domain walls*
- Besides their fundamental interest, can skyrmions actually be used for applications?



[1] F. Garcia-Sanchez *et al.*, New J. Phys. (2016)
[2] J.-V. Kim *et al.*, arXiv:1701.08357

Exploiting the stochastic nature of skyrmion dynamics?



- Idea: Instead of exploiting the deterministic nature (hard), why not use the stochastic nature (easier) instead for applications?

arXiv:1701.07750

Controlling the phase locking of stochastic magnetic bits for ultra-low power computation

Alice Mizrahi^{1,2}, Nicolas Locatelli², Romain Lebrun¹, Vincent Cros¹, Akio Fukushima³, Hitoshi Kubota³, Shinji Yuasa³, Damien Querlioz² & Julie Grollier¹

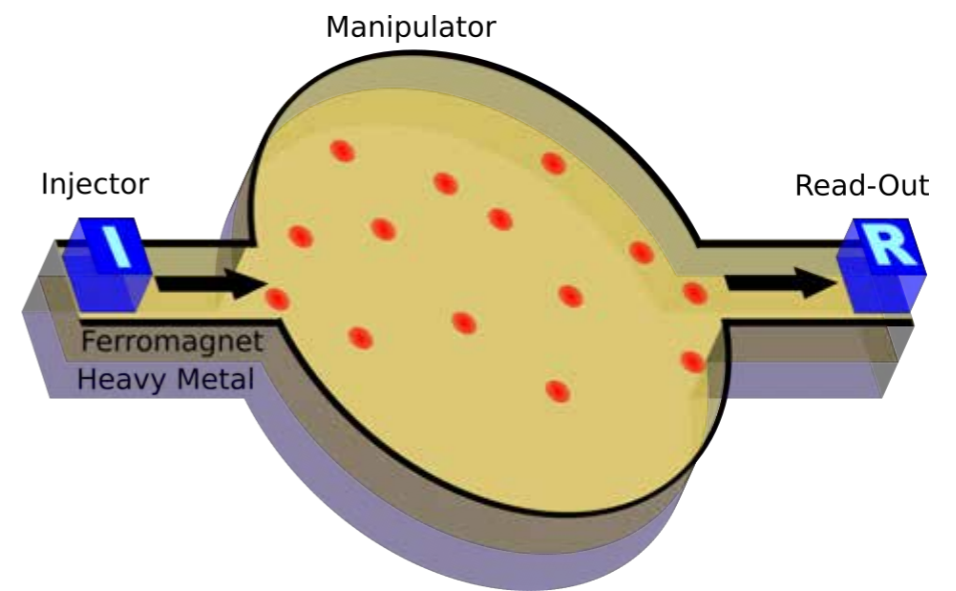
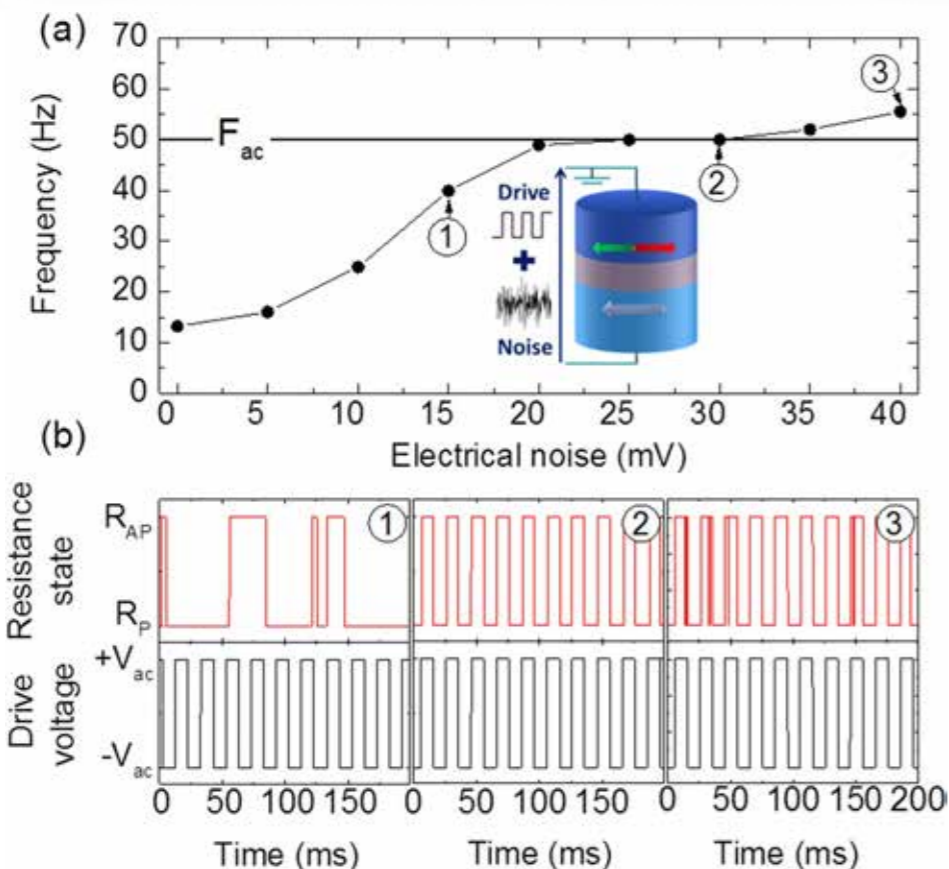
Skyrmion Gas Manipulation for Probabilistic Computing

D. Pinna^{*1}, F. Abreu Araujo¹, J.-V. Kim², V. Cros¹, D. Querlioz², P. Bessiere³, J. Droulez³ and J. Grollier¹

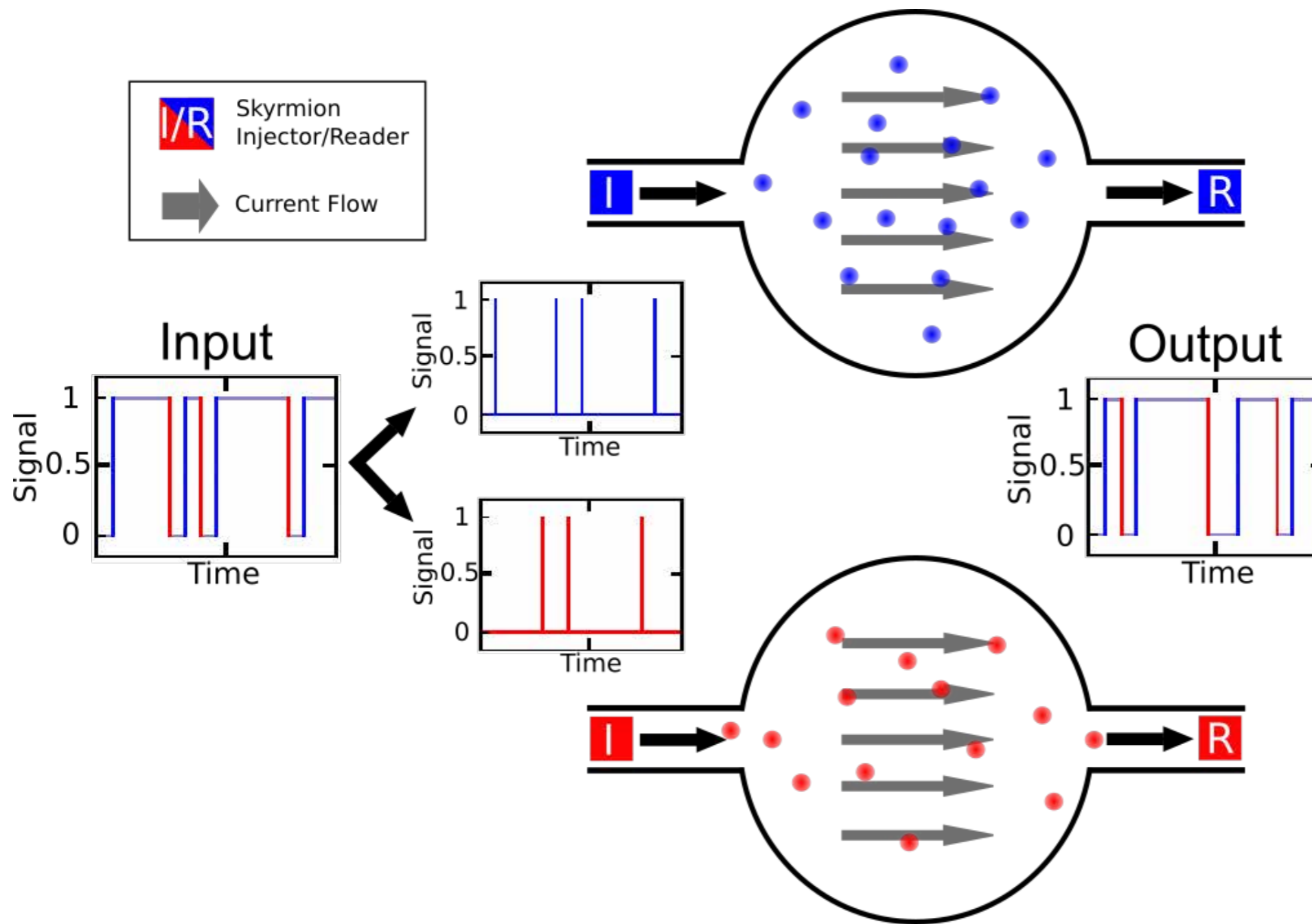
¹Unité Mixte de Physique CNRS, Thales, Univ. Paris-Sud, Université Paris-Saclay, 91767 Palaiseau, France

²Centre for Nanoscience and Nanotechnology, CNRS, Univ. Paris-Sud, Université Paris-Saclay, 91405 Orsay, France

³Institut des Systèmes Intelligents et de Robotique, Université Pierre et Marie Curie, Paris, France



Sci. Rep. 2016



Skyrmion
reshuffler
device

Figure 9: The proposed device consists of two magnetic chambers into which skyrmions are injected depending on the state of an input telegraph noise signal. The net drift of the skyrmion particles due to a constant current flow along with the thermal diffusion in the chambers leads to an exit order that can be significantly different from that of entry. This is employed to reconstruct a new outgoing signal with the same statistical properties as the first as well as being uncorrelated from it.

- Examined boundary edge and disorder-induced confinement effects in ultrathin ferromagnets with perpendicular anisotropy:
 - *Skyrmion oscillators with inhomogeneous polarizers*
 - *Current-induced motion in disordered films*
- Disorder can result in strong pinning, finite threshold currents, stochastic motion in realistic films
 - *Undesired effects for information storage applications, possibly no advantages compared with domain walls*
- Besides their fundamental interest, can skyrmions actually be used for applications?
 - *Stochastic-based paradigms for computing*

